

# Cyber-Physical Computation

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# Table of Contents

Cyber-Physical Systems

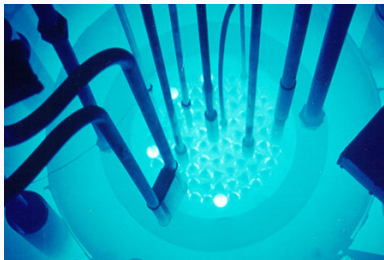
Contents of the course

Logistics

# Cyber-Physical Systems



Digital devices that interact with their physical environment



## Another example of a cyber-physical system



SpaceX's Starship | SN8

## ... and yet some other cases

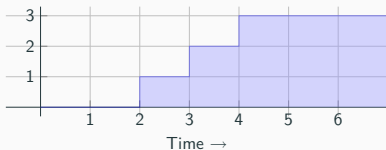
- Semi-autonomous self-driving systems
- (Crewed) spacecrafts

# The three ingredients of cyber-physical systems

- Concurrency
- Communication
- Hybrid interaction

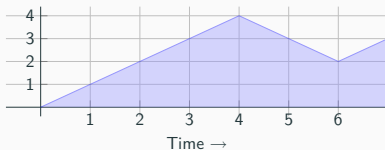
# Computer Science meets Analysis

Wait Calls



```
(wait 2); x := x + 1; (wait 1) ...
```

Differential Statements

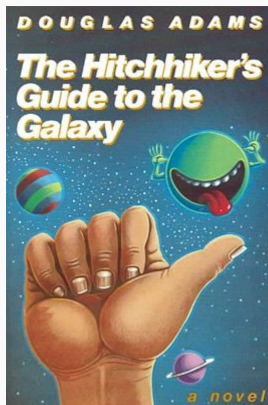


```
while (true) {  
  if  $v \leq 2$   
    then ( $\dot{v} = 1$  for 2)  
    else ( $\dot{v} = -1$  for 2) }
```

# A particle and its orbital trajectory – what can go wrong?

```
x := -1; v := 0; a := 1;
while true do {
    if x <= 0 then a := 1; else a := -1;
    x' = v, v' = a for 0.5;
}
```





What is actually **computable** ?

Genesis: David Hilbert and its  
*Entscheidungsproblem* (circa 1928)



Fuelled the appearance of first models of computation (circa 1936)

- Turing machines: state-based, part of **automata** theory
- $\lambda$ -calculus: function-based, prototypical **programming** lang

**Computable** if encodable as a Turing machine or (equivalently) as a  $\lambda$ -term



# Table of Contents

Cyber-Physical Systems

Contents of the course

Logistics

We will study diverse models of cyber-physical computation

- (timed) automata,
- a hybrid while-language,
- $\lambda$ -calculus extended with computational effects (monads!)

We will study diverse models of cyber-physical computation

- (timed) automata,
- a hybrid while-language,
- $\lambda$ -calculus extended with computational effects (**monads!**)

and often make detours through the **mathematical foundations** of automata and programming language theory ...

We will get acquainted with diverse tools

- **Uppaal** verification of real-timed systems modelled by (networks of) timed automata
- **Lince** agile analysis of cyber-physical systems modelled by a hybrid while-language
- **Haskell** a platform to study  $\lambda$ -calculus with effects

# How deep will we go into the rabbit hole?

Our learning path will intersect theory and practice, from the very basics to the state-of-the-art — we will face current limitations and see what challenges lie ahead





Cyber-Physical Systems

Contents of the course

Logistics

Two individual assignments (about the modelling and analysis of cyber-physical systems)

# Materials and Contacts

Relevant class material and announcements posted on the website

<https://haslab.github.io/MFP/>

e-mail: [nevrenato@di.uminho.pt](mailto:nevrenato@di.uminho.pt)

office hours: wednesday afternoon (please send an email the day before if you wish to meet)



Edward A Lee, *Cyber-physical systems-are computing foundations adequate*, Position paper for NSF workshop on cyber-physical systems: research motivation, techniques and roadmap, vol. 2, Austin, TX, 2006, pp. 1–9.



Ragunathan Rajkumar, Insup Lee, Lui Sha, and John Stankovic, *Cyber-physical systems: the next computing revolution*, Proceedings of the 47th design automation conference, 2010, pp. 731–736.