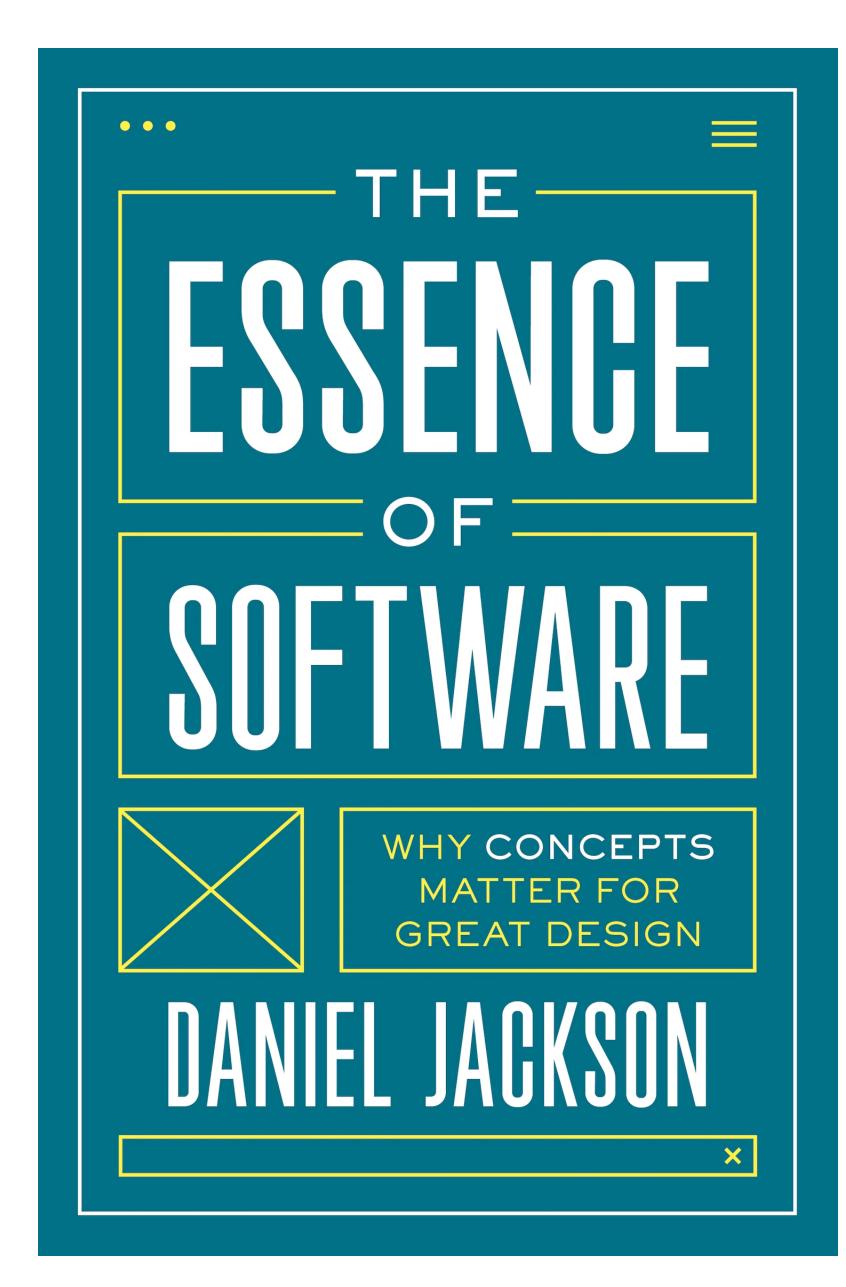
# Behavioral design with Alloy

Alcino Cunha

# Software concepts

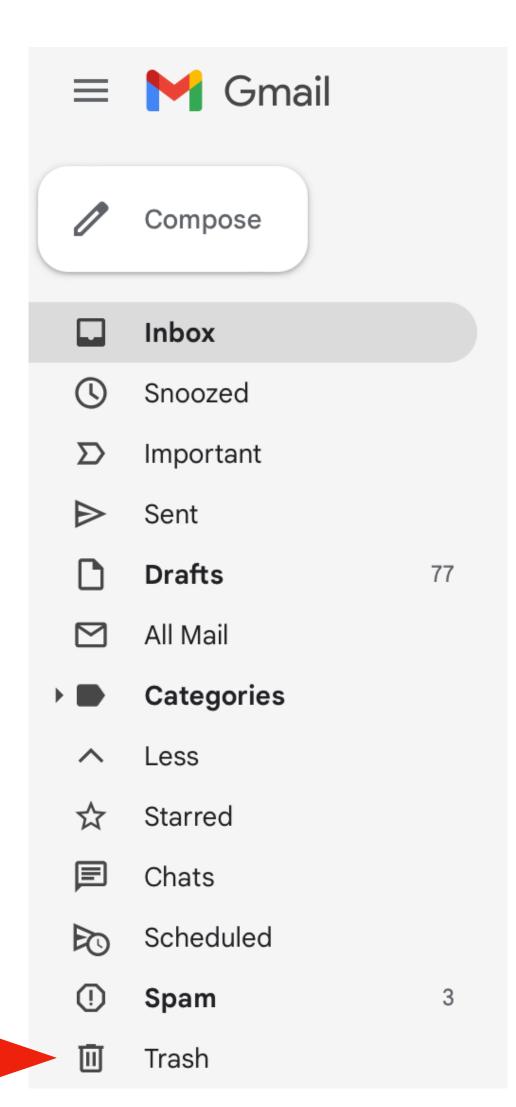


## Concepts

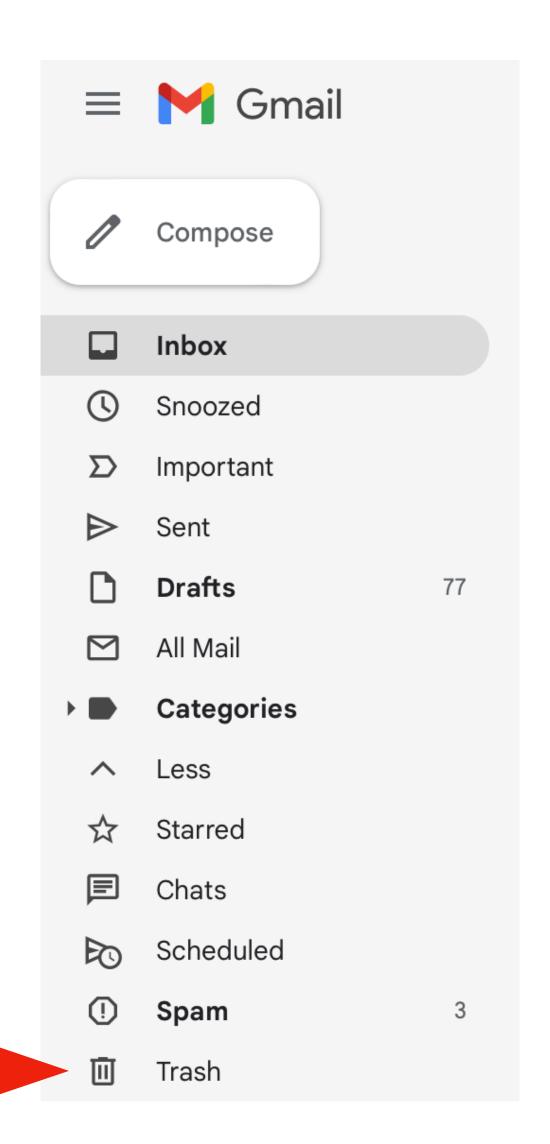
- Apps are made of recurring concepts
- Each concept is a self-contained unit of functionality with a clear purpose
- Concepts work together to provide the app overall functionality
- But can be understood independently of one another

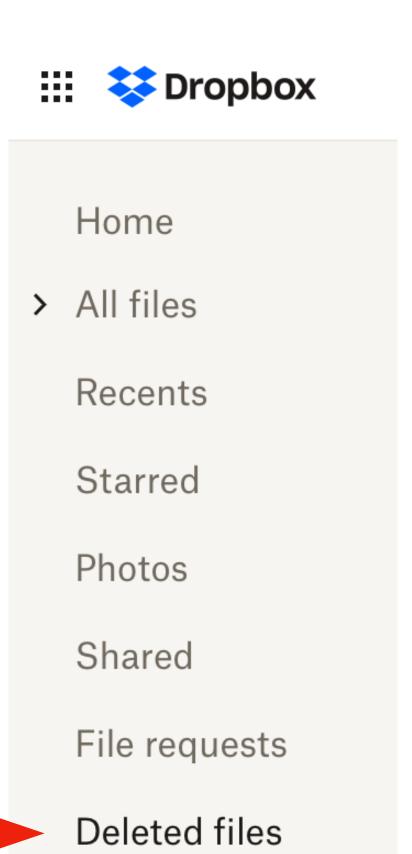


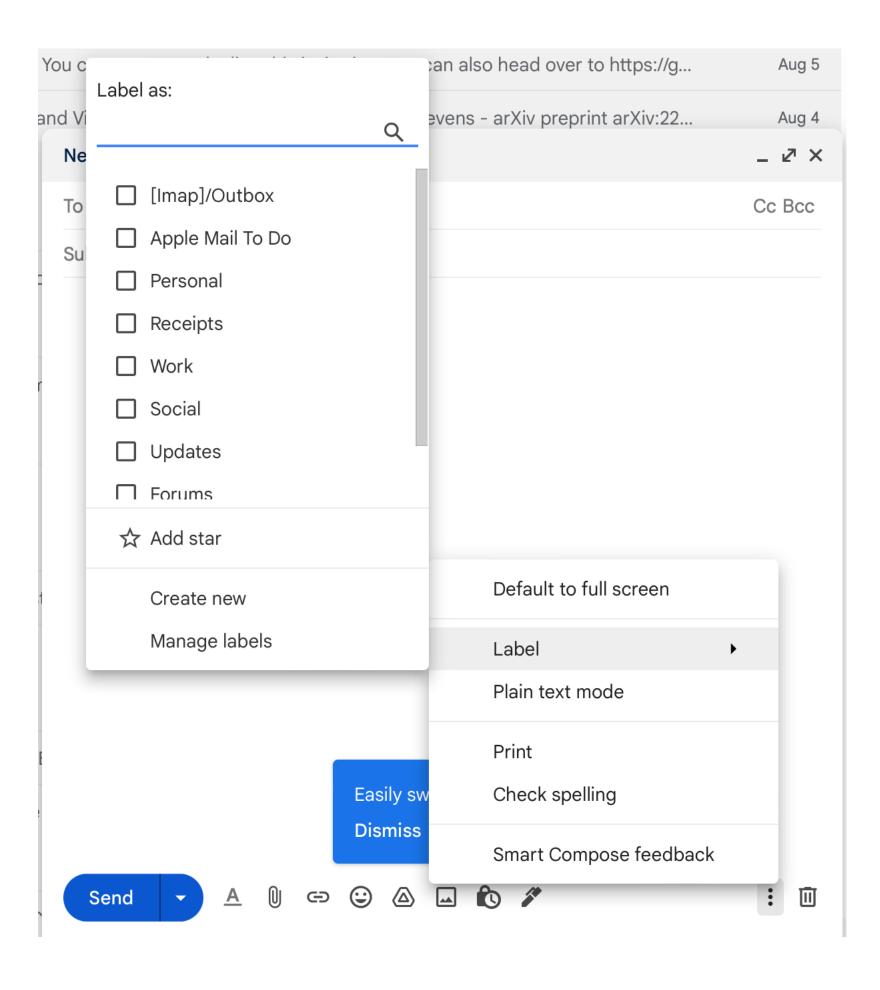






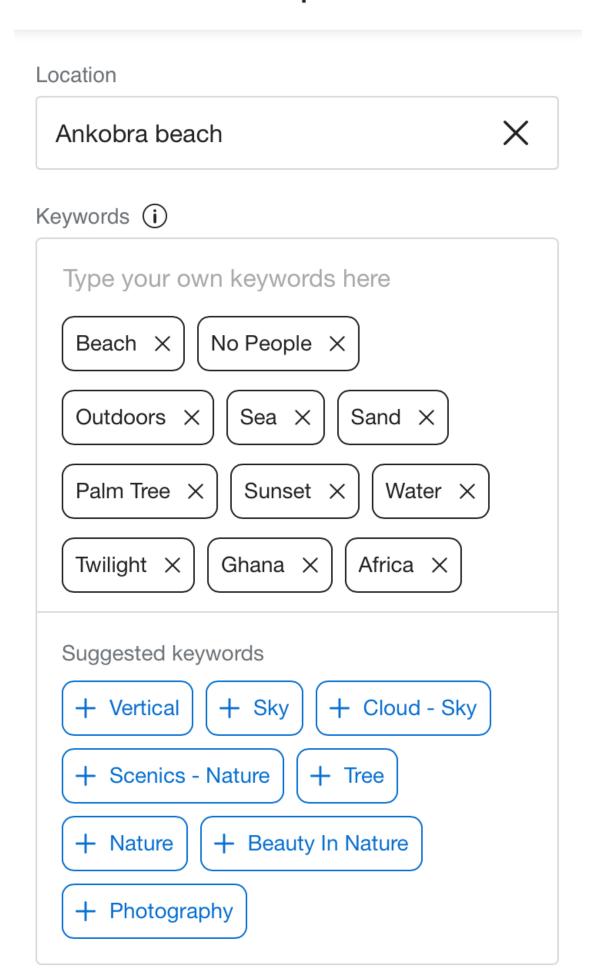


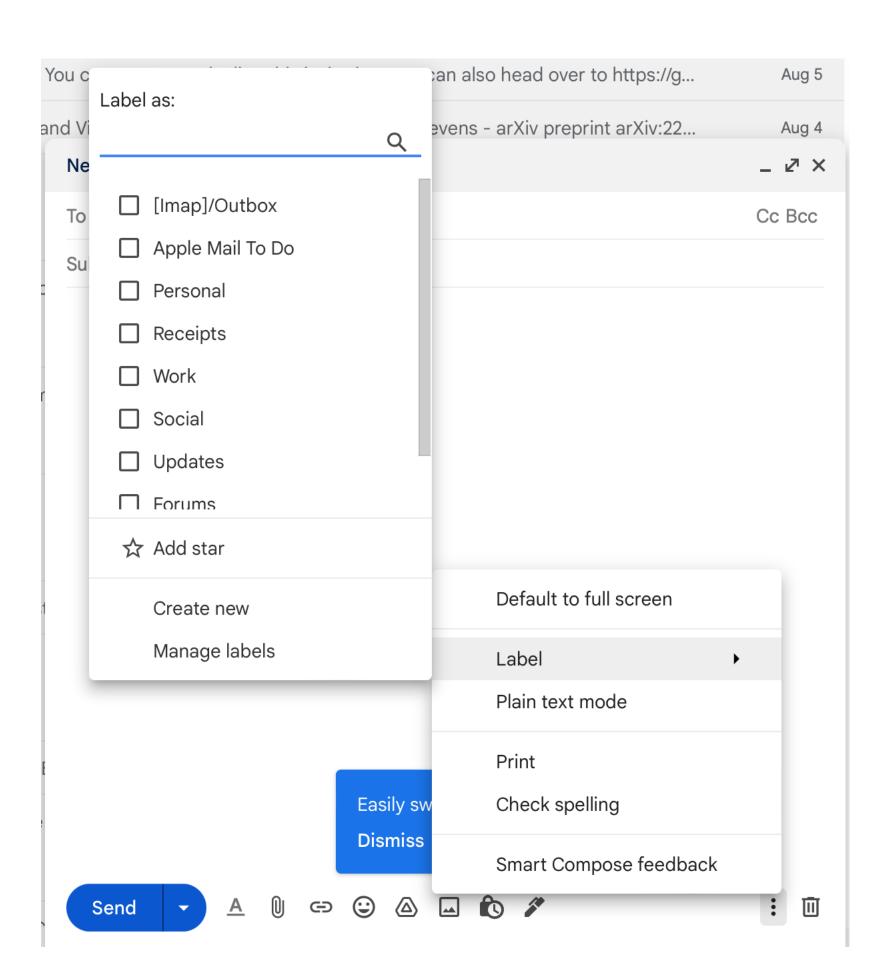




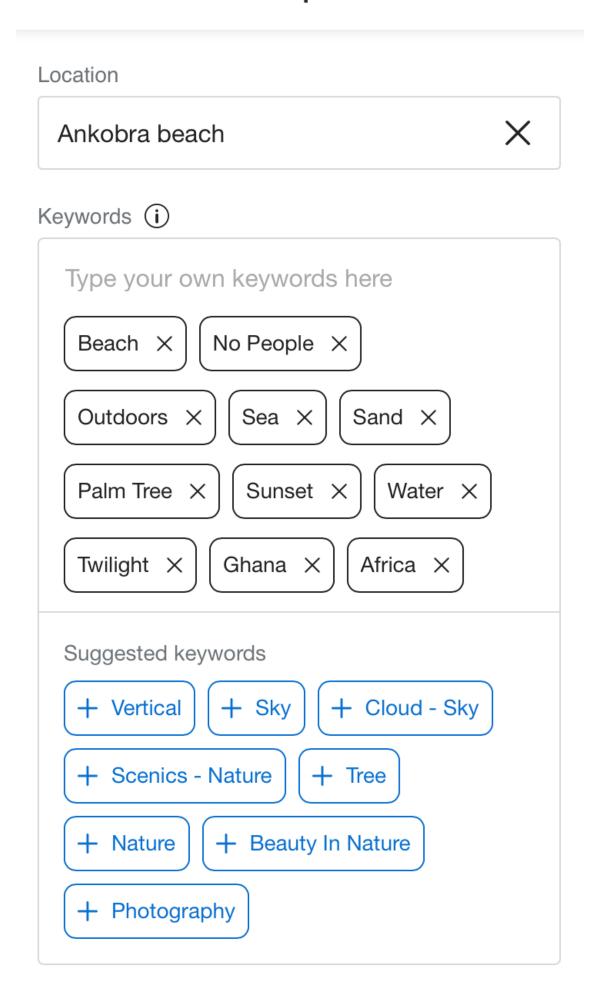
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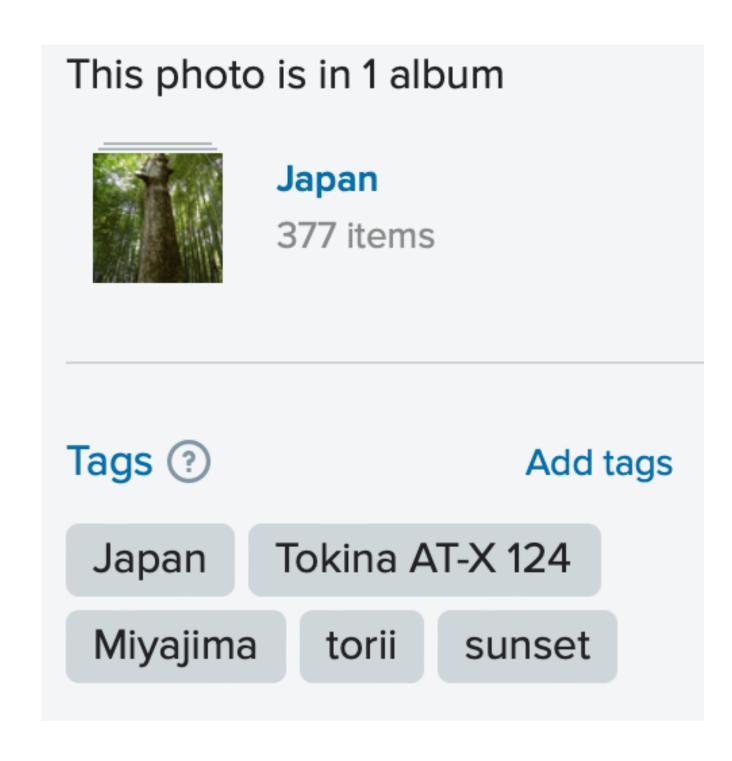
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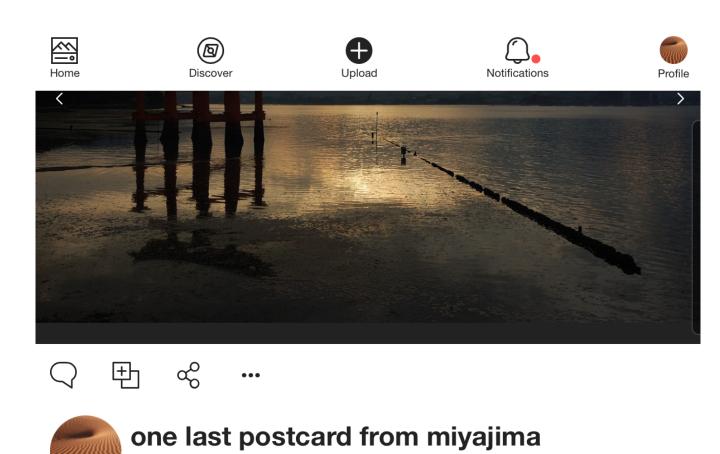




#### **Edit 1 photo**







Taken: Aug 17, 2008 Uploaded: almost 11 yrs ago

Miyajima, Japan [2008]

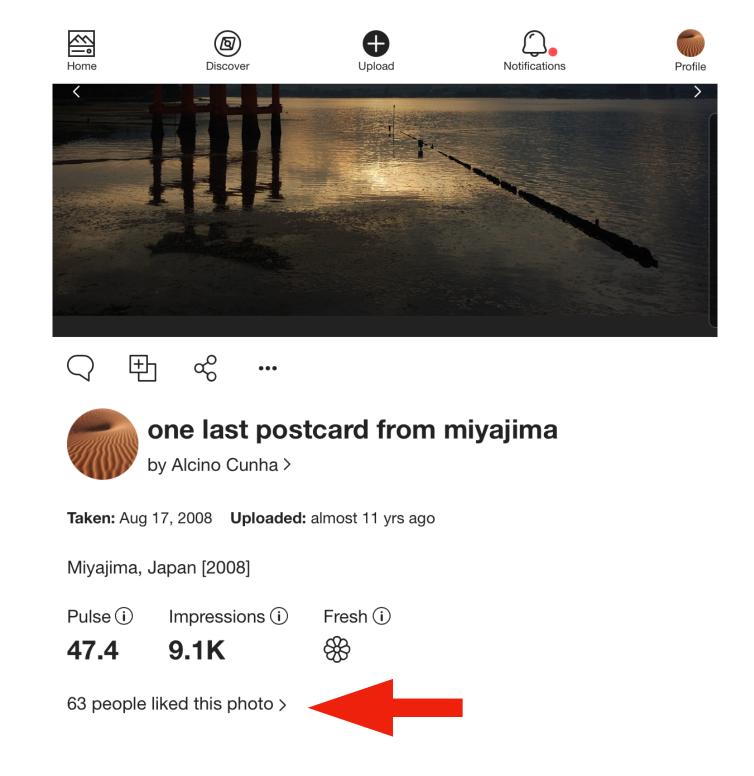
Pulse (i) Impressions (i) Fresh (i)

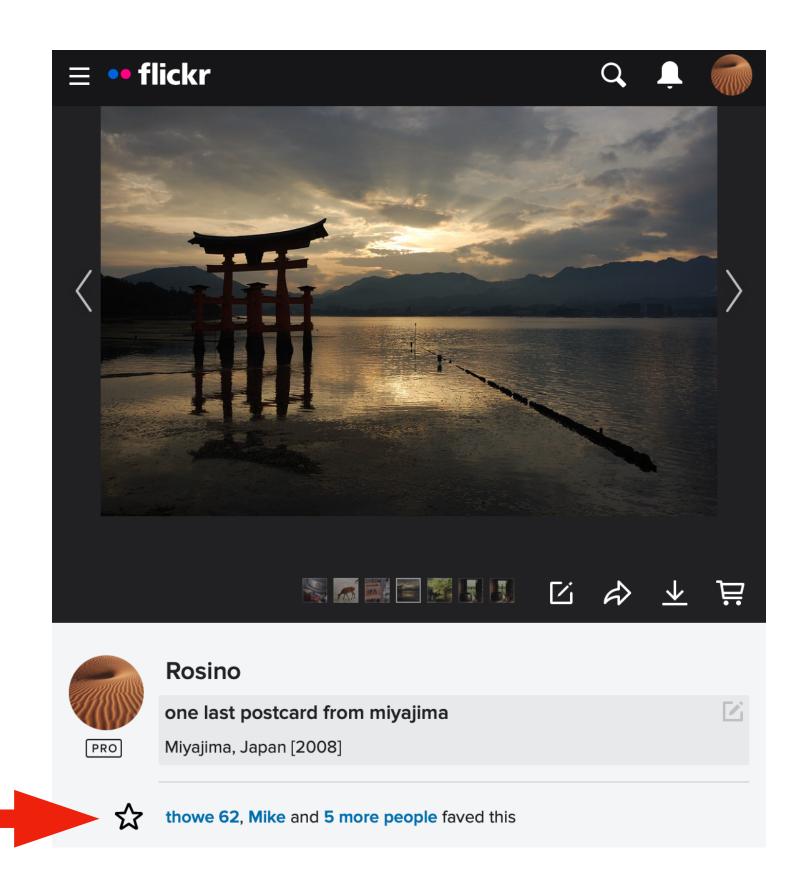
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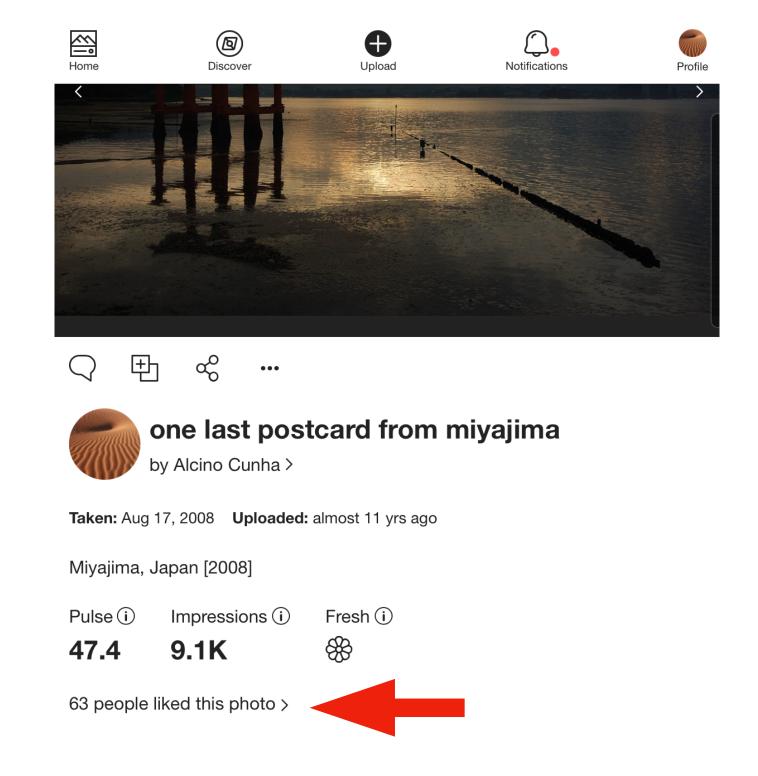
by Alcino Cunha >

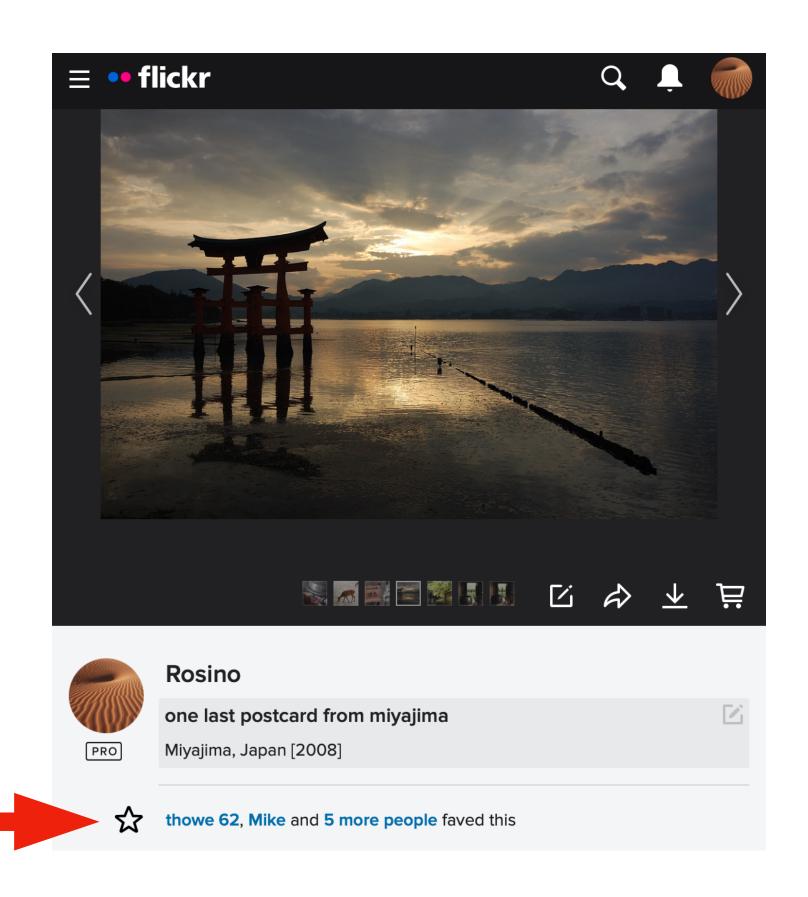
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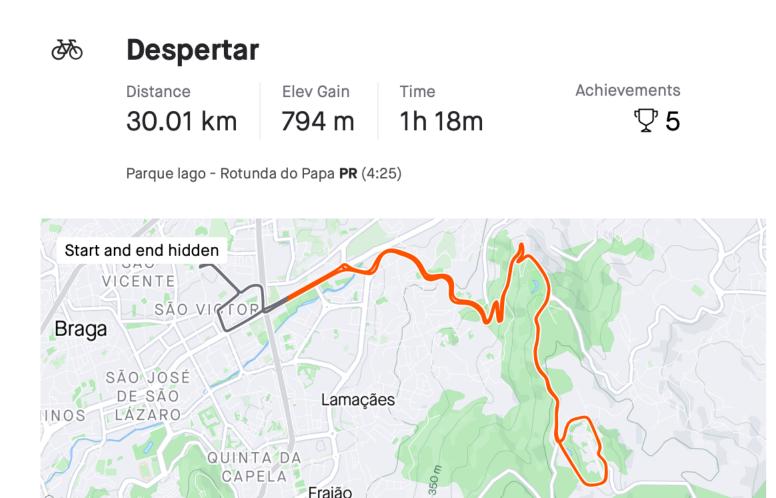












ి Only your followers can view this activity. It won't appear on segment leaderboards and may

not count toward some challenges.

11 kudos

## Concept design

- Identify a clear purpose
- Choose the appropriate state and actions to fulfill that purpose
- The focus is on ensuring correctness and reusability

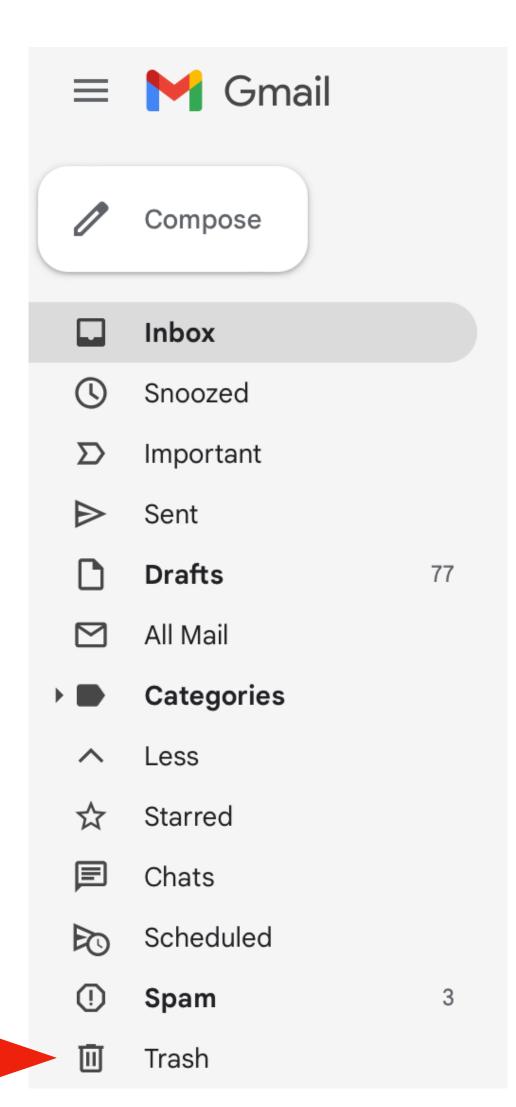
## App design

- Identify the core concepts
- Compose them, maybe providing new functionality
- The focus is on exploration

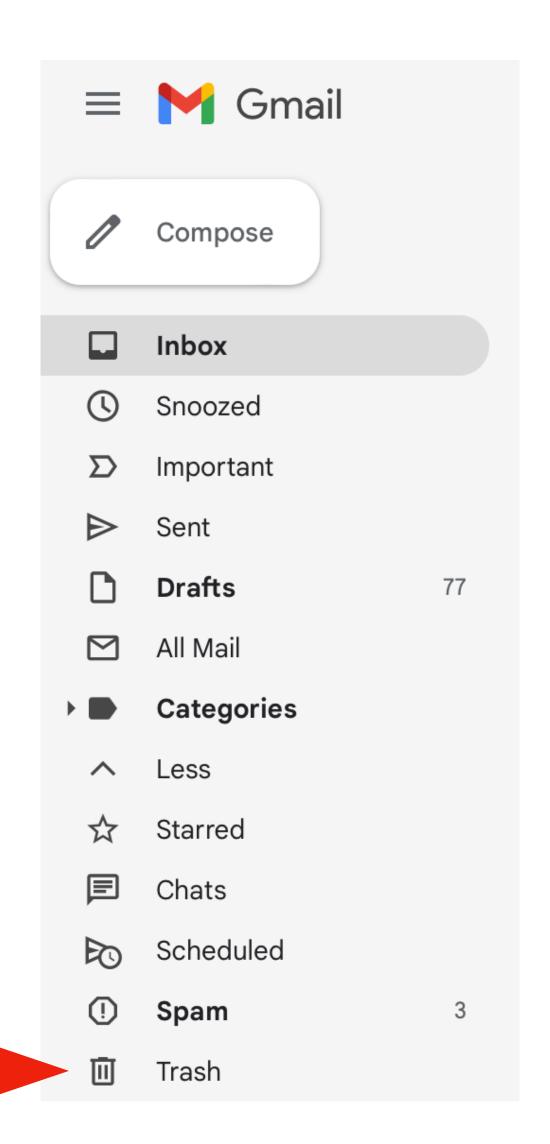
## Modeling Concepts

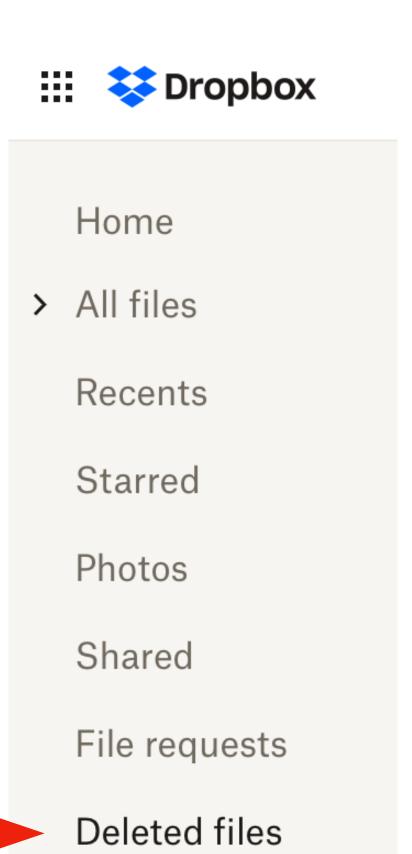






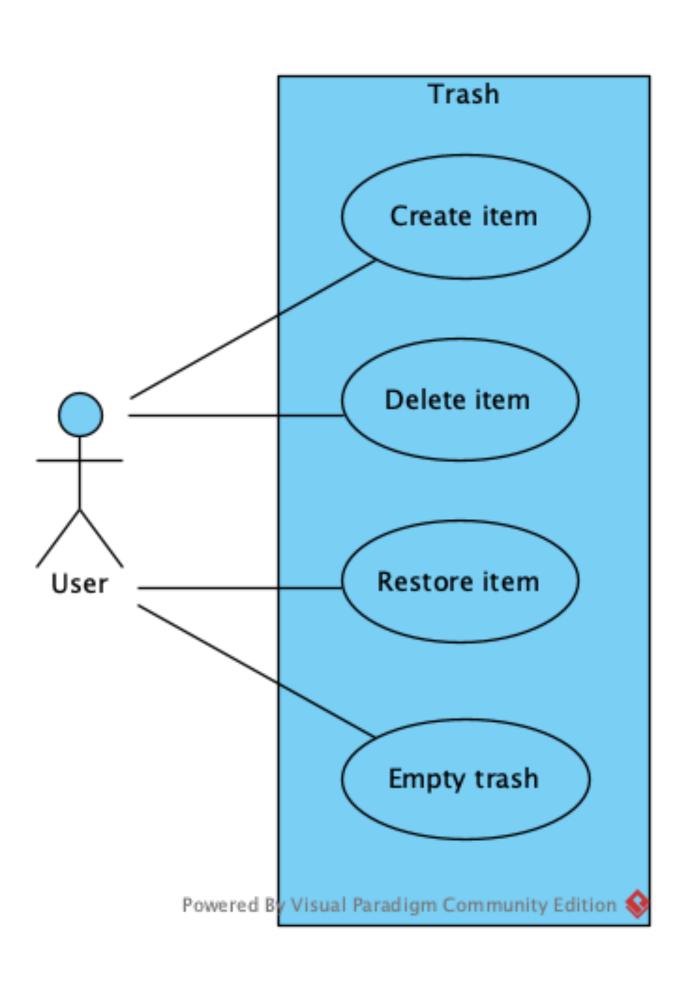




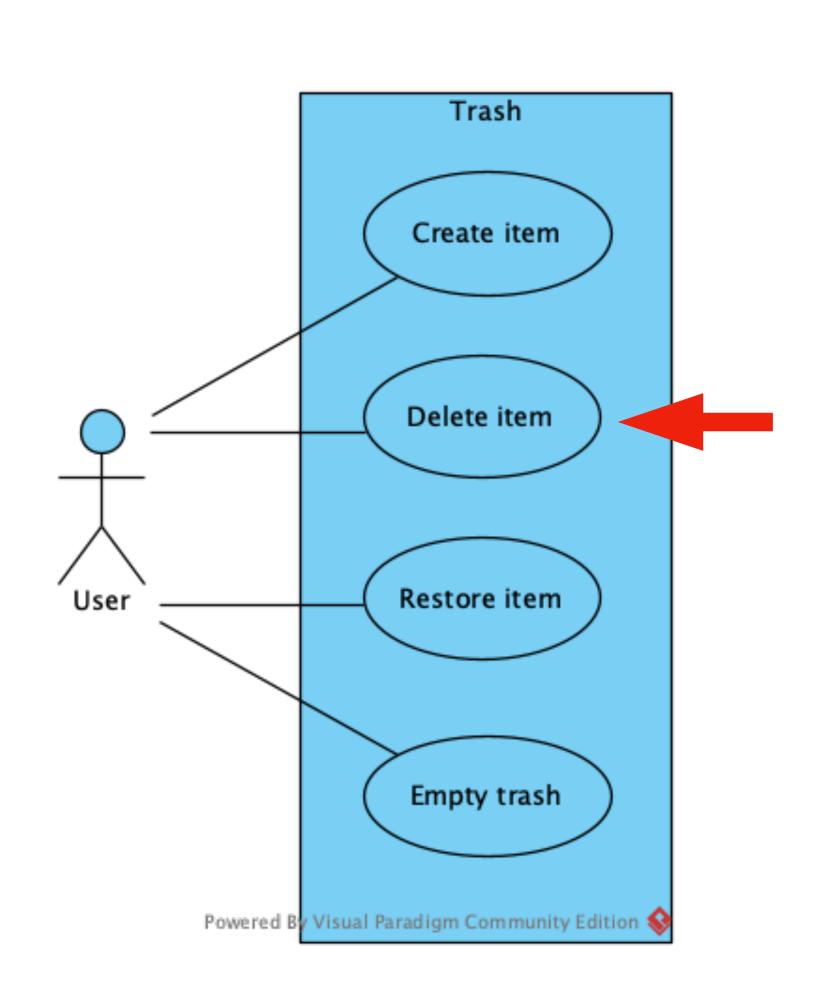


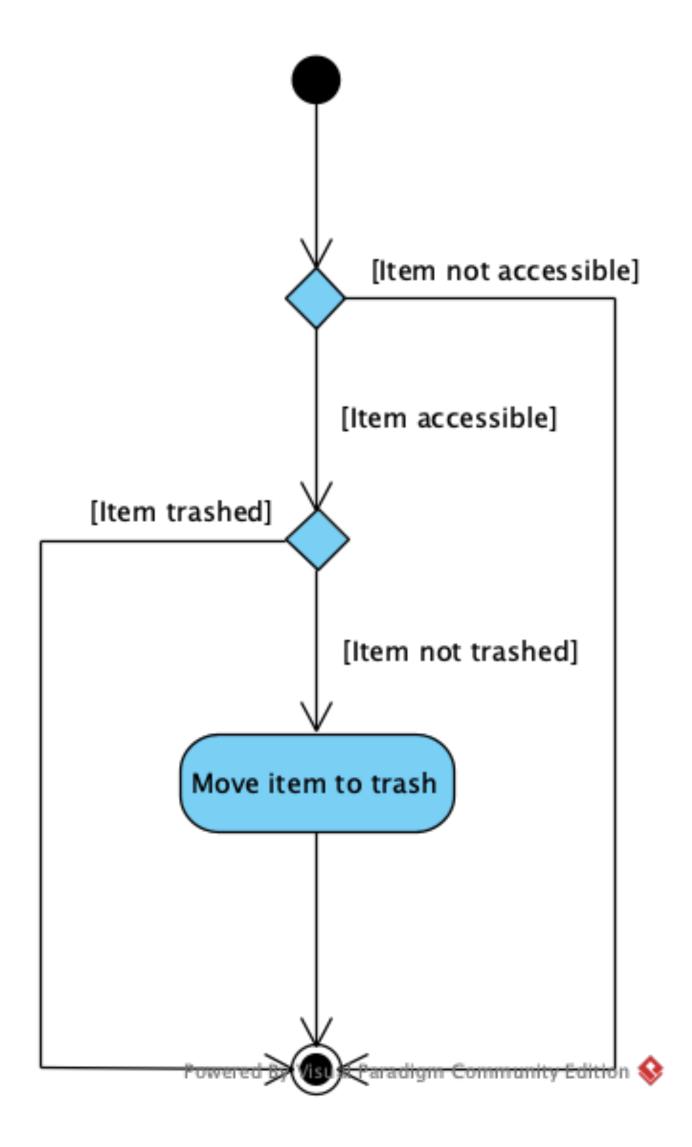
## Trash modeling a la UML

# Trash modeling a la UML



# Trash modeling a la UML





# Trash modeling a la Jackson

```
concept trash [Item]
purpose
  to allow undoing of deletions
state
  accessible, trashed : set Item
actions
  create (x : Item)
    when x not in accessible or trashed
    add x to accessible
  delete (x : Item)
    when x in accessible but not trashed
    move x from accessible to trashed
  restore (x : Item)
    when x in trashed
    move x from trashed to accessible
  empty ()
    when some item in trashed
    remove every item from trashed
operational principle
  after delete(x), can restore(x) and then x in accessible
  after delete(x), can empty() and then x not in accessible or trashed
```

## Concept modeling a la Jackson

- Name
  - Optionally parametrized by types that can be specialized when composing
- Purpose
  - A clear reason why you might want it
- State + Actions
  - A description of the concept behavior using a transition system
- Operational principle
  - Properties that show how the purpose is fulfilled by the actions

# Transition systems

## Transition systems

- A popular model to describe the behavior of a system
- A model is often a synonym for a transition system
- There are many variants and related formalisms
  - Labeled transition systems
  - Kripke structures
  - Finite state machines
  - Hybrid and timed automata

- ...

## States, transitions, and traces

#### States

- A state is a possible valuation to the structures of the system
- Initial states describe how the system starts

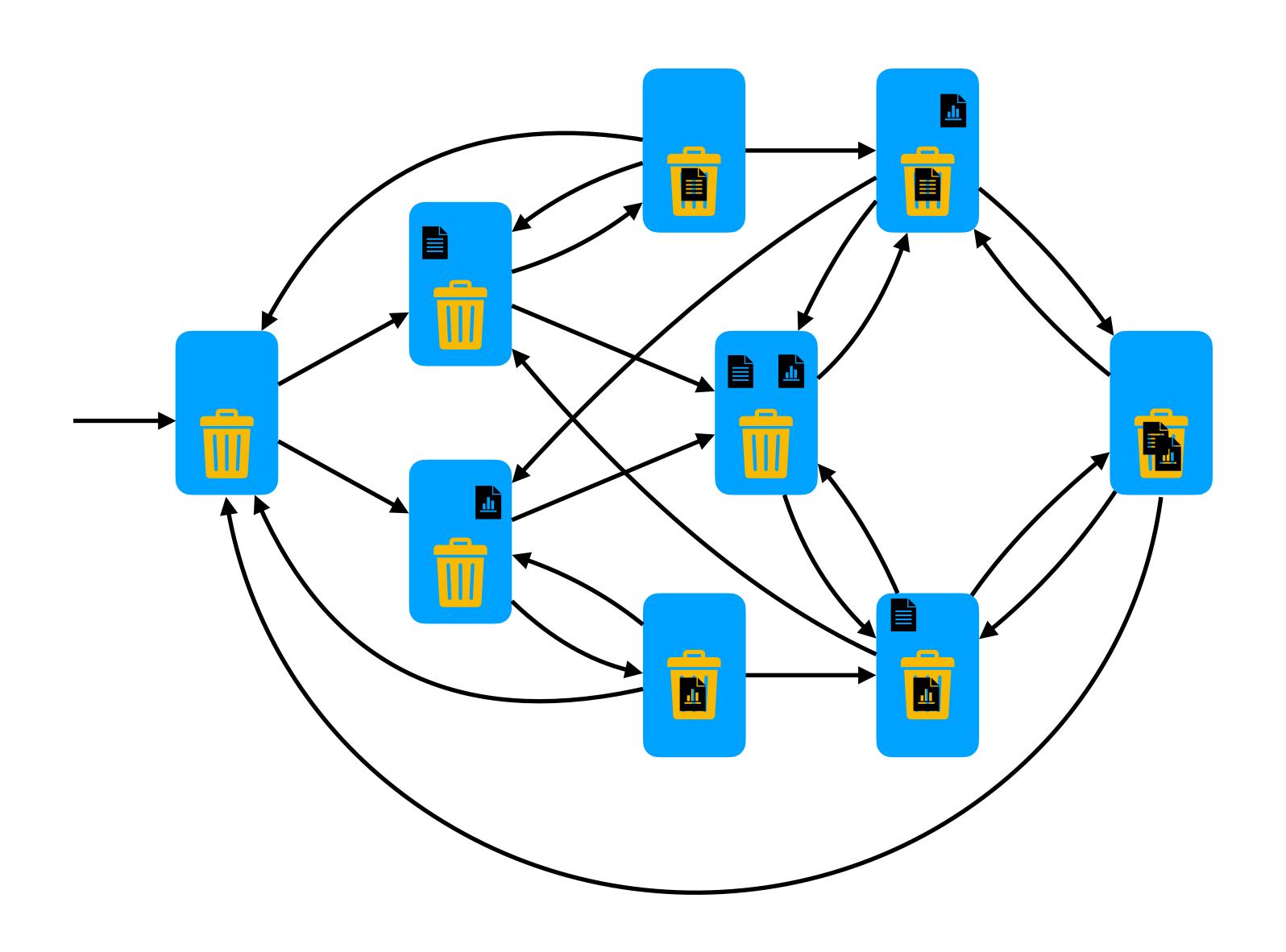
#### Transitions

- A transition is a possible evolution between states
- Transitions originate from actions of the system or the environment

#### Traces

- A trace is a sequence of states, describing a possible execution
- A valid trace in a transition system is a path starting in an initial state

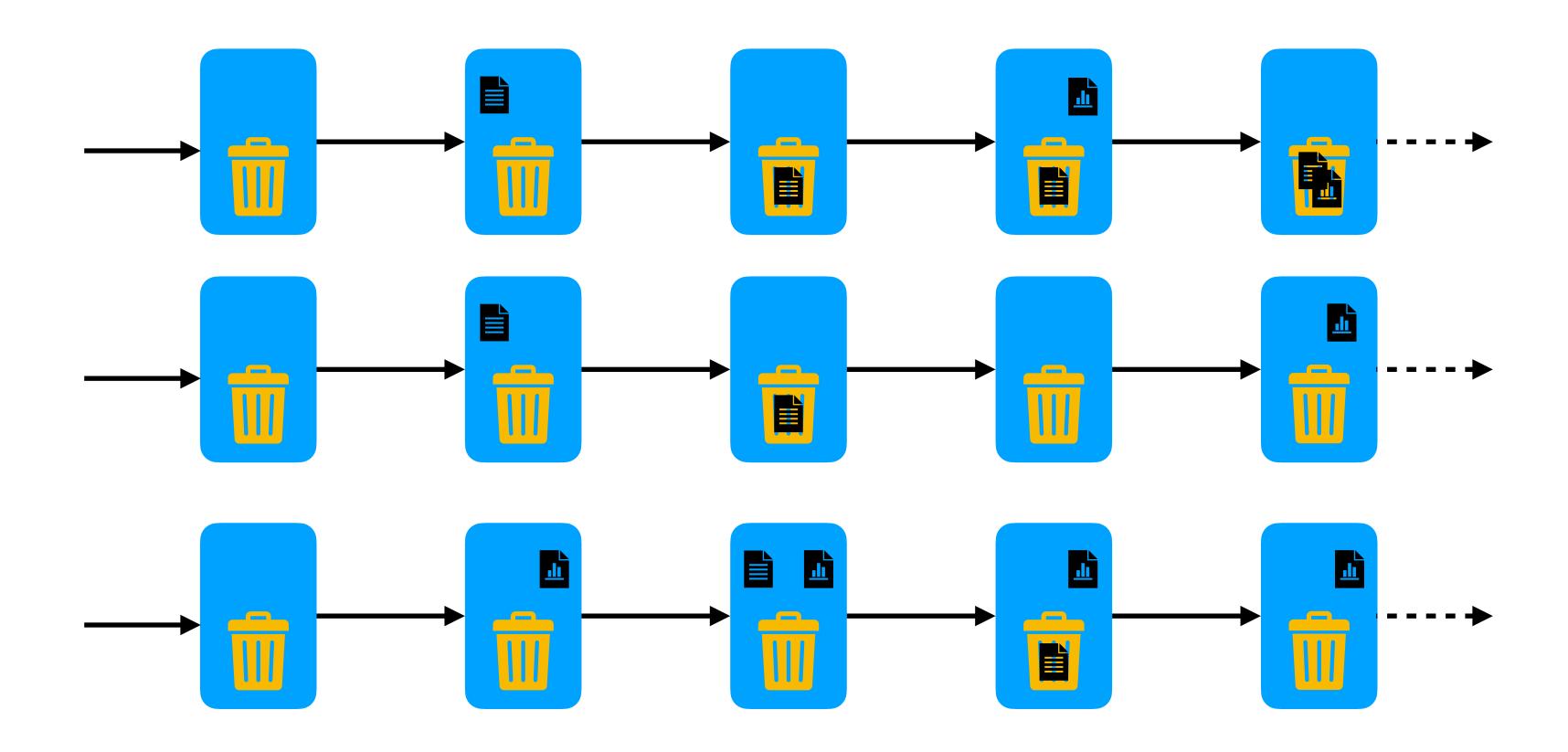
# Trash transition system



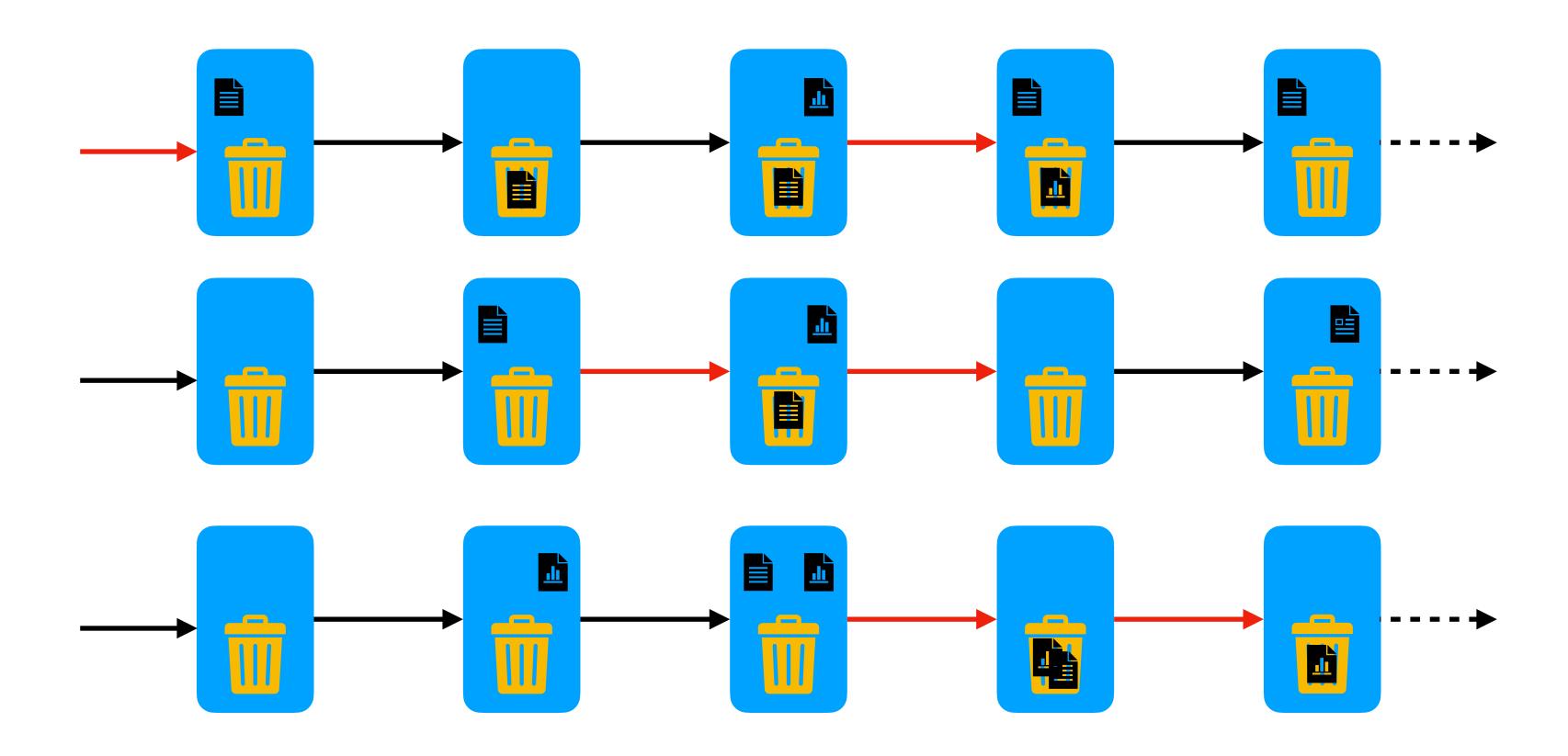
## Declarative modeling

- It is possible to describe a transition system by specifying instead which are its valid traces
- This requires specifying a property whose validity is established in a trace and not just in a single state
- The specification of properties about traces requires some sort of temporal logic

#### Valid trash traces



#### Invalid trash traces



# Specifying transition systems

# Mutability

- In Alloy 6 mutable signatures and fields can be declared with keyword var
  - Static field inside mutable signature yields a warning
  - Static signature extending or subset of a mutable one also yields a warning

### Trash states

```
sig Item {}
var sig Accessible in Item {}
var sig Trashed in Item {}
```

#### Instances

- When mutable structures are declared, instances are infinite traces
- Analysis commands only return traces that can be represented finitely
  - Traces that loop back at some point
- Static signatures and fields are known as the configuration and have the same value in all states
- If there are mutable top-level signatures, **univ** (and **iden**) are also mutable

# Temporal logic

- Alloy 6 also supports linear temporal logic
- Temporal logic adds temporal operators to relational logic
- They allow us to "quantify" the validity of a formula over the different states of a trace
- A formula without temporal operators is only required to hold in the initial states
- Alloy 6 has both future and past temporal operators
- It also has the prime operator that denotes the value of a term in the next state

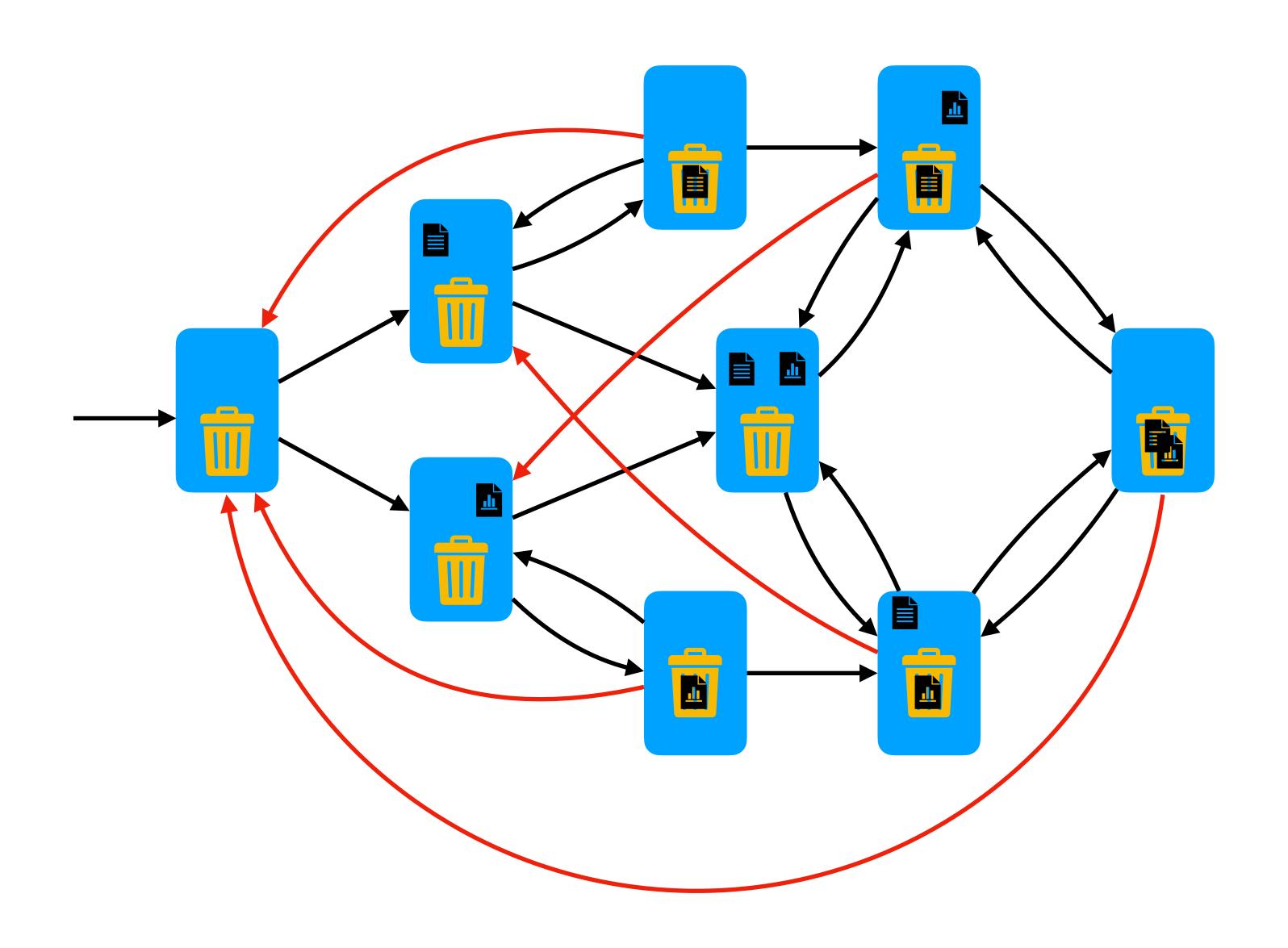
# Always, eventually, and prime

```
always \phi \phi is true in all future states eventually \phi is true in some future state R' The value of R in the next state
```

### Actions

- A set of transitions can be specified declaratively with an action
  - A formula without temporal operators, but including primed and unprimed variables
  - A condition without primed variables is a *guard* that specifies when is the action enabled
  - A condition with a primed variable is an effect that specifies what are the possible values for that variable after the action occurs
  - If a variable does not change, a frame condition should be included stating that the next value of the variable is the same
- By combining actions with the always temporal operator we can specify a system behavior
- Actions were first introduced by Leslie Lamport in the Temporal Logic of Actions

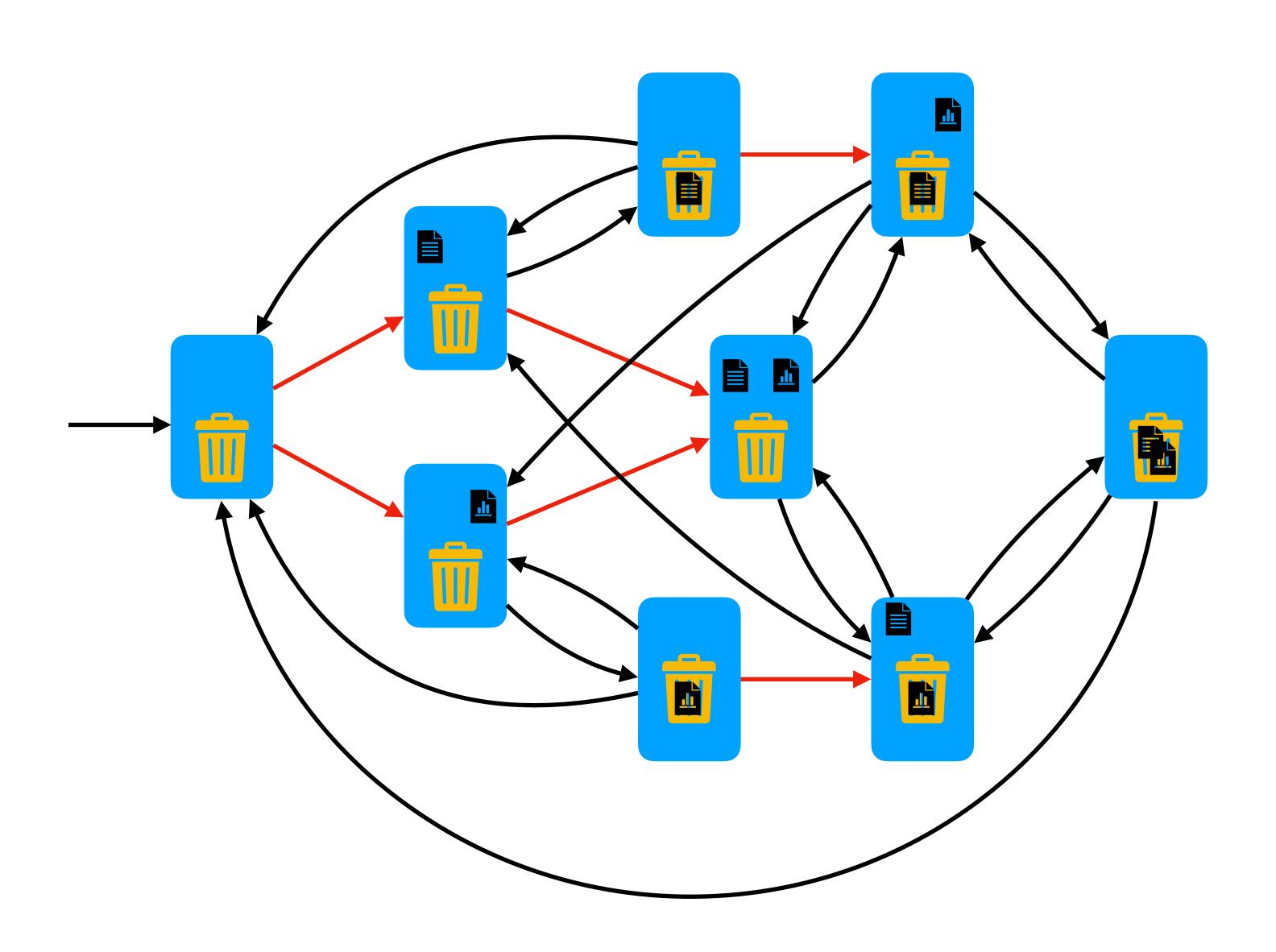
# Empty trash



# Empty trash

```
pred empty {
    // guard
    some Trashed
    // effect
    no Trashed'
    // frame condition
    Accessible' = Accessible
}
```

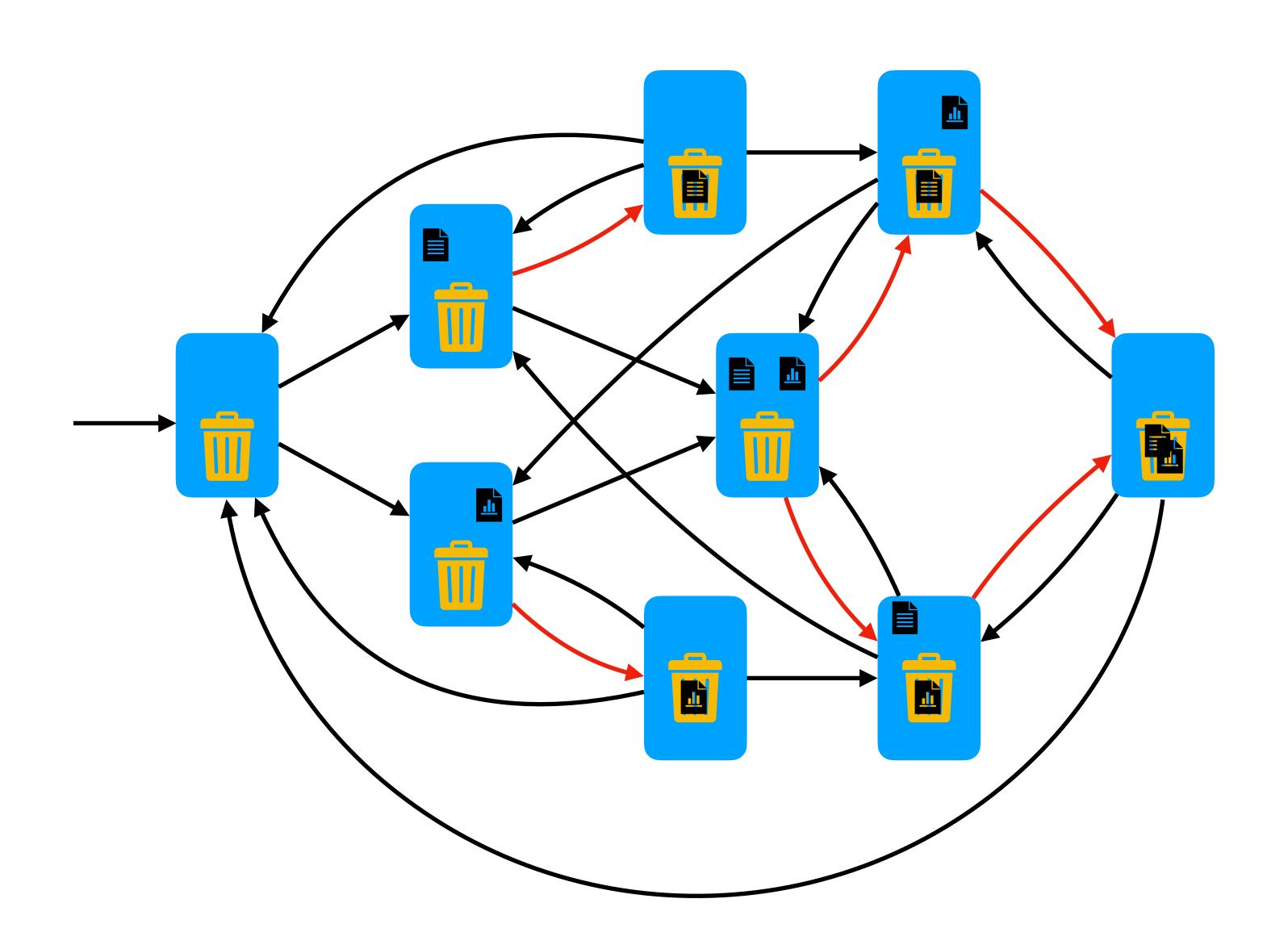
## Create item



#### Create item

```
pred create [i : Item] {
    // guard
    i not in Accessible + Trashed
    // effect
    Accessible' = Accessible + i
    // frame condition
    Trashed' = Trashed
}
```

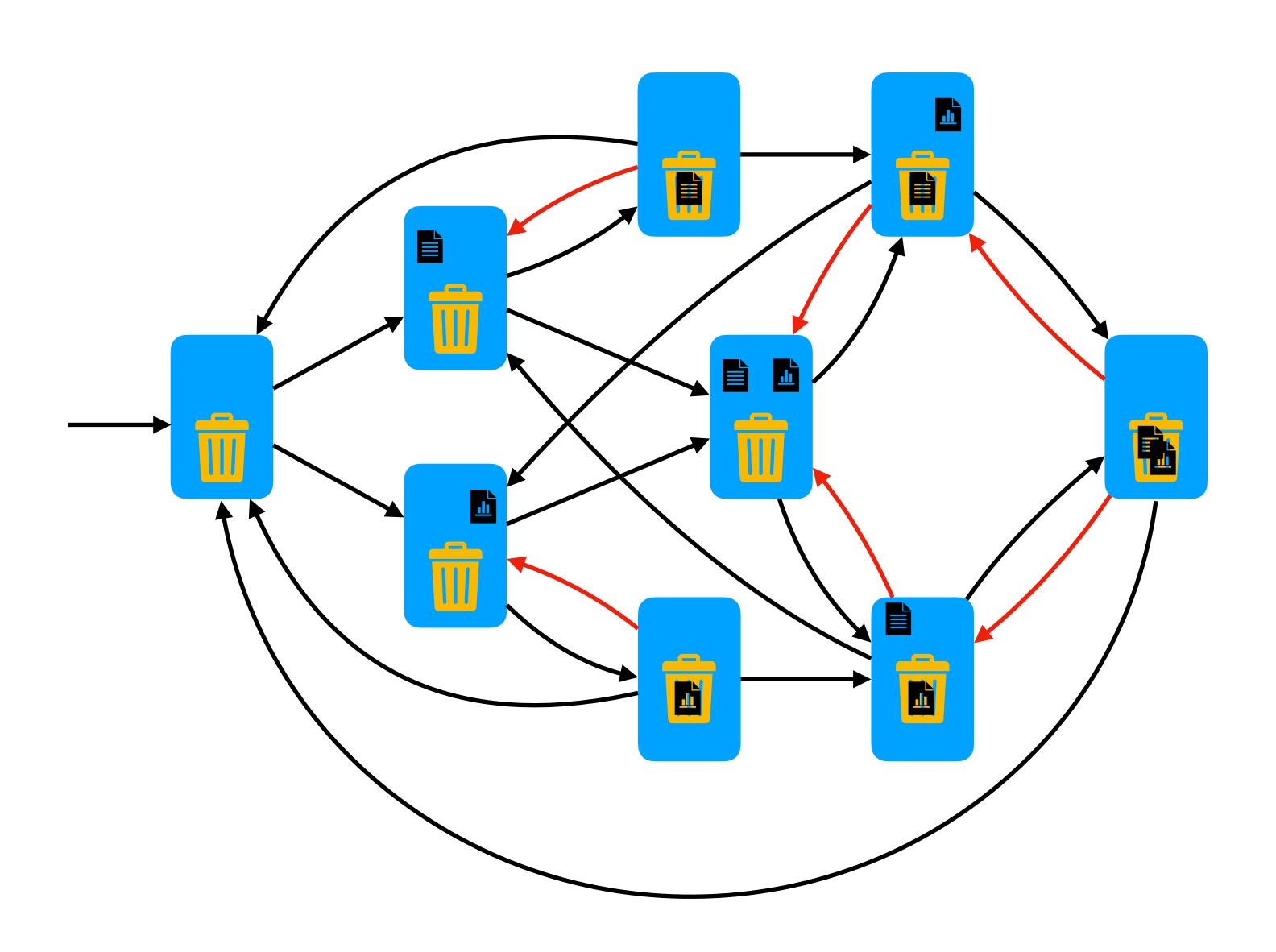
## Delete item



#### Delete item

```
pred delete [i : Item] {
    // guard
    i in Accessible
    // effects
    Accessible' = Accessible - i
    Trashed' = Trashed + i
}
```

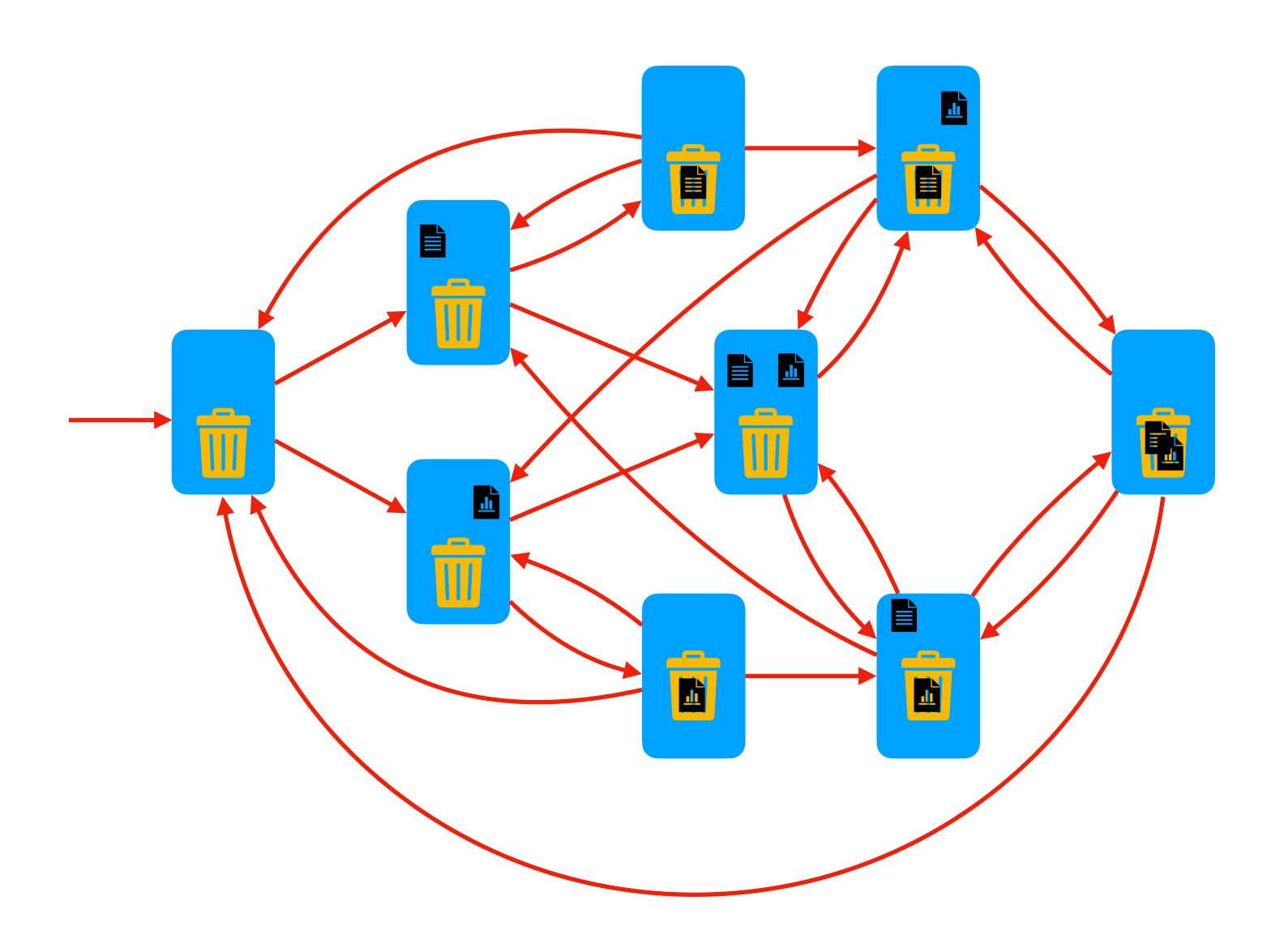
## Restore item



#### Restore item

```
pred restore [i : Item] {
    // guard
    i in Trashed
    // effects
    Accessible' = Accessible + i
    Trashed' = Trashed - i
}
```

## Trash behavior



#### Trash behavior

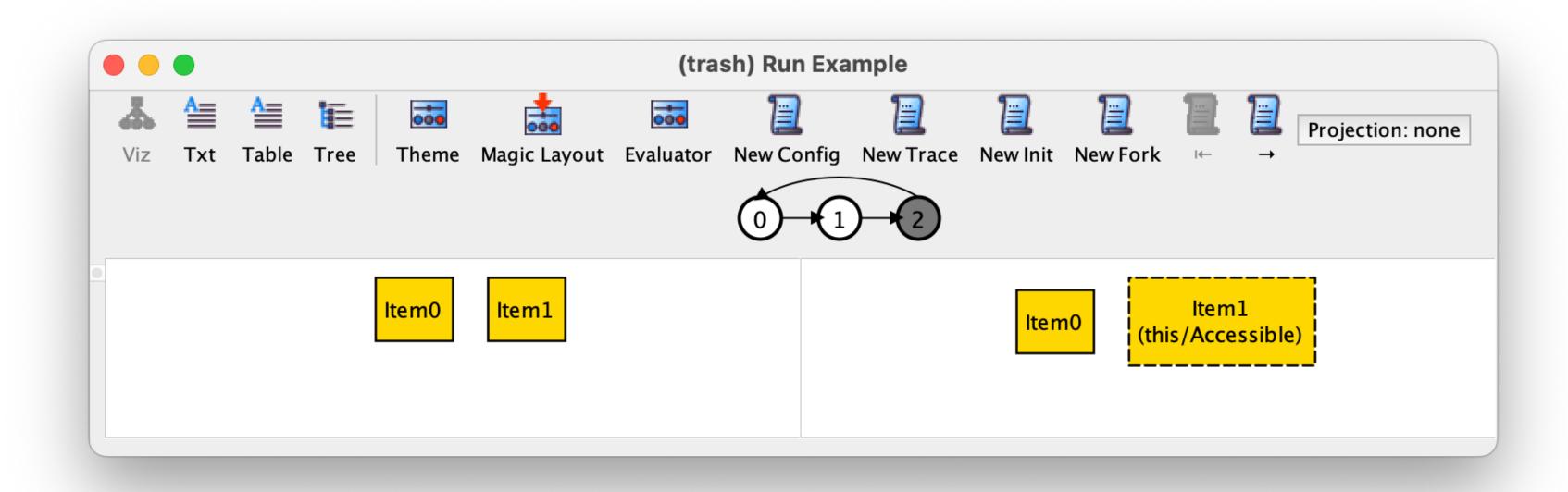
```
fact Behavior {
  // initial state
  no Accessible
  no Trashed
  // possible transitions
  always {
    (some i : Item | create[i] or delete[i] or restore[i])
    or
    empty
```

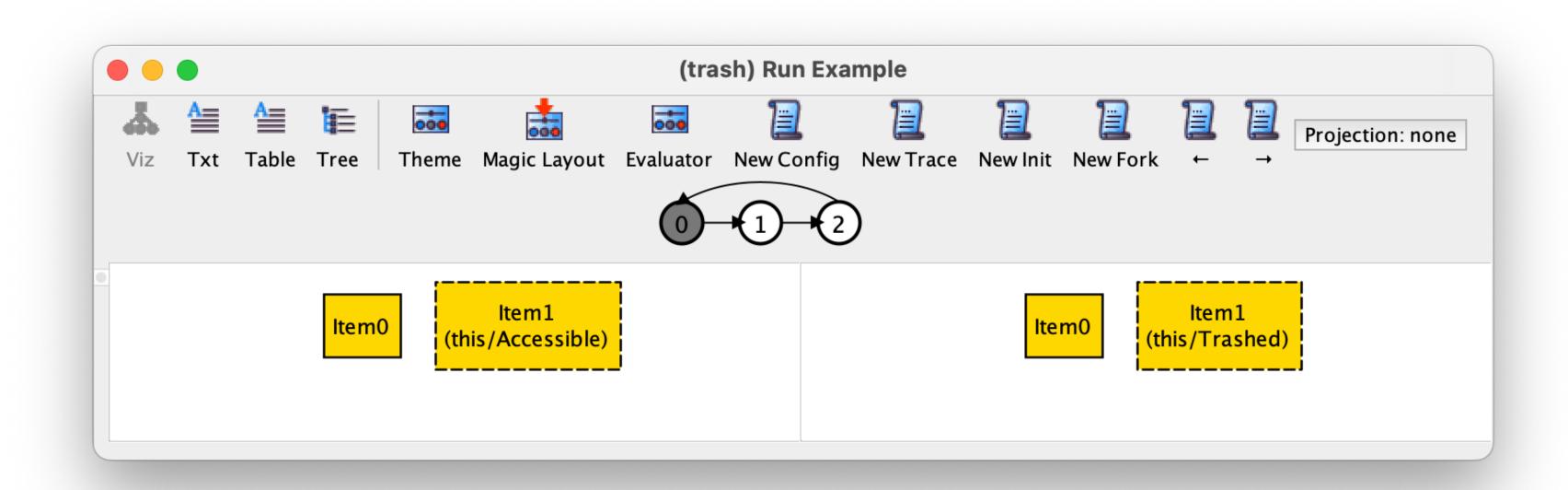
## Validation

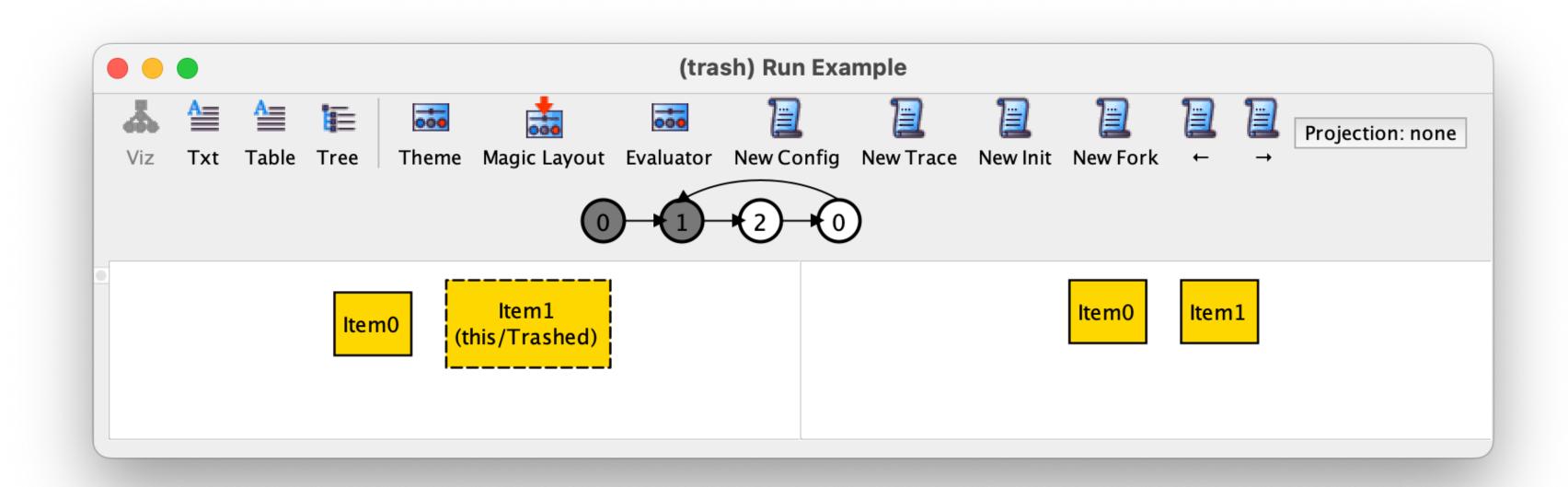
#### Run commands

- As usual, run commands can be used to validate the model
- The scope of a mutable signature defines the maximum number of different atoms in the full trace, not a maximum per state

- The visualizer depicts two consecutive states of the trace side-by-side
  - By default mutable structures are depicted with dashed lines
- A representation of the infinite trace is shown above
  - Different states have different numbers
  - The loop back is explicitly depicted
  - Clicking on a state focus on that (and the succeeding) state
  - It is possible to move forwards and backwards in the trace with → and ←







### Simulation

- It possible to perform "simulation" with the New instance buttons
  - New config, returns a trace with a different configuration (a different value to the immutable structures)
  - New trace, returns any different trace with the same configuration
  - New init, returns a trace with the same config, but a different initial state
  - New fork, returns a trace with the same prefix, but a different next state

## Simulation



# Specifying scenarios

- A formula can be given in a run command to look for specific scenarios
- Keyword expect can be used to distinguish positive and negative scenarios

## Semi-colon

 $\phi$  ;  $\psi$ 

 $\psi$  is valid after  $\phi$ 

## Some trash scenarios

```
run Scenario1 {
  some i : Item {
   create[i]; delete[i]; restore[i]; delete[i]; empty
} expect 1
run Scenario2 {
  some disj i,j : Item {
   create[i]; delete[j]
} expect 0
run Scenario3 {
  some i : Item {
   create[i]; delete[i]; empty
} for 1 Item expect 1
```

# Stuttering

# A clock specification

```
pred clock_spec {
   h = 12 and m = 0
   always {
      m'=(m+1)%60 and
      m=59 implies h'=(h%12)+1 else h'=h
   }
}
```



# Ceci n'est pas une montre?!

check clock\_spec

#### Executing "Check clock\_spec"

Solver=sat4j Steps=1..10 Bitwidth=4 MaxSeq=4 SkolemDepth=1 Symmetry=20 Mode=batch 1..2 steps. 55 vars. 12 primary vars. 59 clauses. 3ms.

Counterexample found. Assertion is invalid. 3ms.



# A clock specification

```
pred clock_spec {
    h = 12 and m = 0
    always {
        m'=(m+1)%60 and
        m=59 implies h'=(h%12)+1 else h'=h
        or
        m'=m and h'=h
}
```



### Another clock

check clock\_spec

#### Executing "Check clock\_spec"

Solver=sat4j Steps=1..10 Bitwidth=4 MaxSeq=4 SkolemDepth=1 Symmetry=20 Mode=batch 1..10 steps. 151901 vars. 1875 primary vars. 413006 clauses. 1042ms. No counterexample found. Assertion may be valid. 298ms.



# Stuttering

- Stuttering can represent events by the environment or by other components of the system (not yet modeled)
- Stuttering enables refinement
  - adding detail or new components to a system
  - namely, it enables concepts to be composed to build apps
- In terminating systems, stuttering enables traces to be infinite

# Trash stuttering

```
pred stutter {
   Accessible' = Accessible
   Trashed' = Trashed
}
```

#### Trash behavior

```
fact Behavior {
  // initial state
  no Accessible
  no Trashed
  // possible transitions
  always {
    (some i : Item | create[i] or delete[i] or restore[i])
    or
    empty
    or
    stutter
```

## Verification

# Model checking

- Model checking is the process of automatically verifying if a temporal logic specification holds in a finite transition system model of a system
  - If the specification is false a counter-example is returned
  - A finite transition system may have infinite non-looping traces
  - But every invalid specification can be falsified with a looping trace
- Complete or unbounded model checking explores all traces of the transition system
- Bounded model checking explores all traces up to a given maximum number of transitions before looping back

### Verification

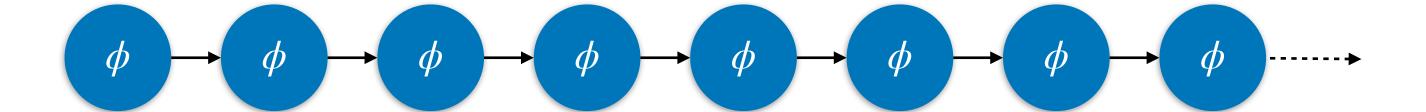
- check commands can be used to verify temporal assertions
- The default verification mechanism is bounded model checking
  - The default maximum number of transitions is 10
  - This can be changed by setting a scope for steps
- Alloy 6 also supports unbounded model checking
  - Activated by the special scope 1.. steps
  - Requires model checkers nuXmv or NuSMV to be installed

# Future temporal operators

```
always \phi\phi will always be trueeventually \phi\phi will eventually be trueafter \phi\phi will be true in the next state\psi until \phi\phi will eventually be true and \psi is true until then\phi releases \psi\psi can only stop being true after \phi
```

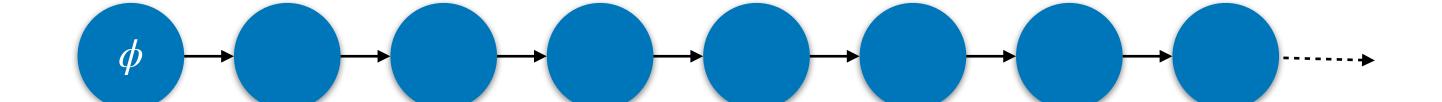
## Future operators

always  $\phi$ 

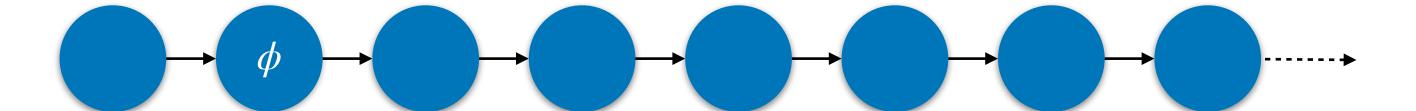


eventually  $\phi$ 

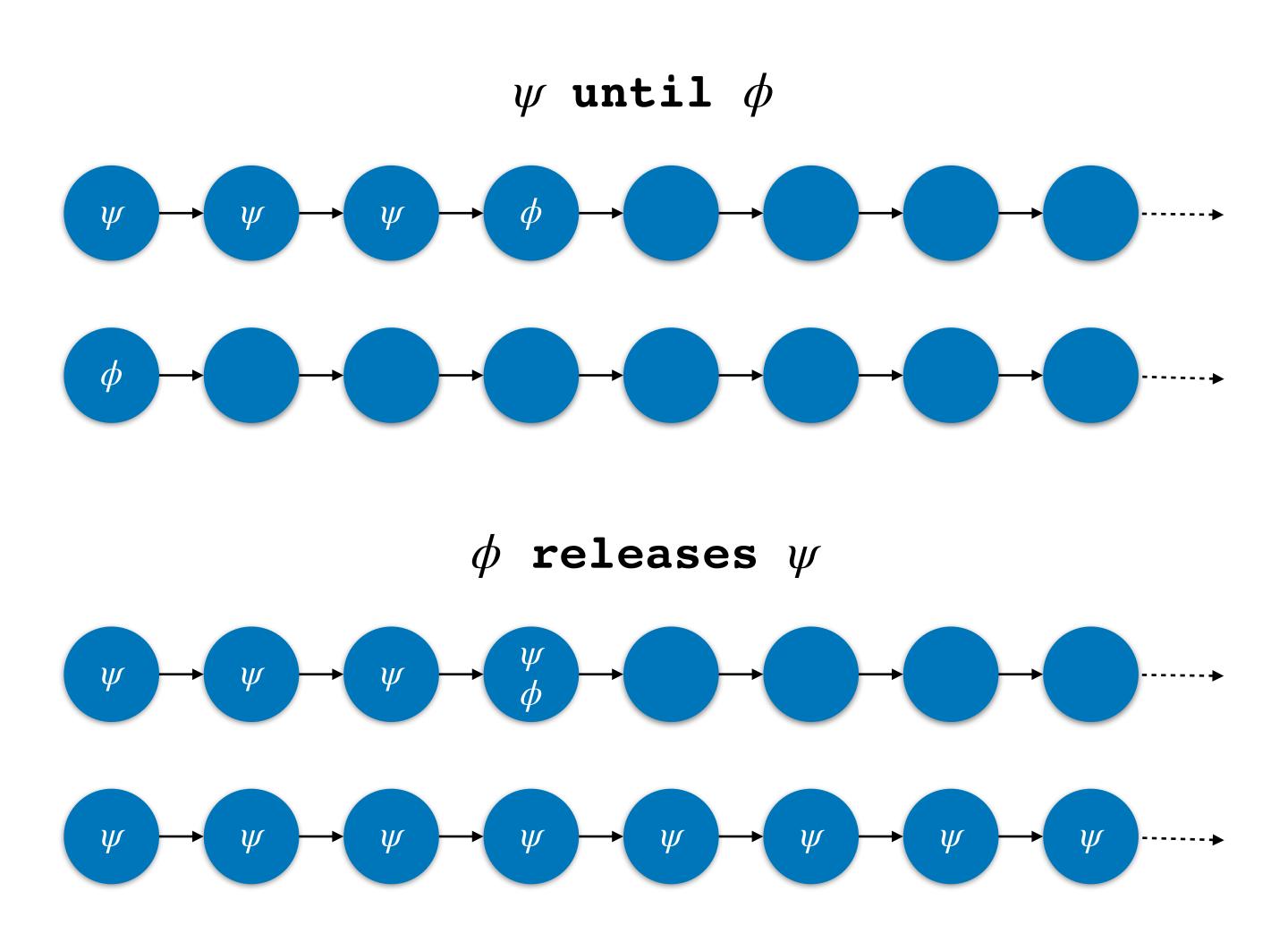




after  $\phi$ 

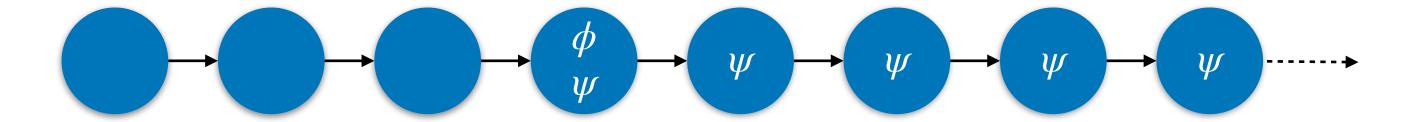


## Future operators

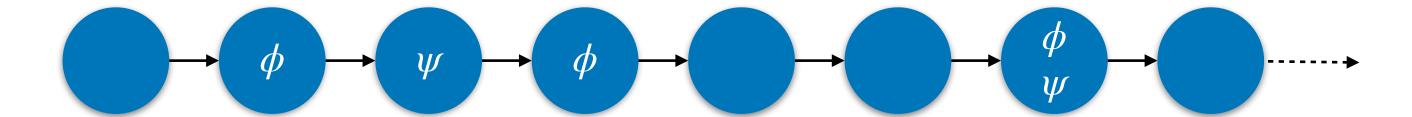


## Mixing operators

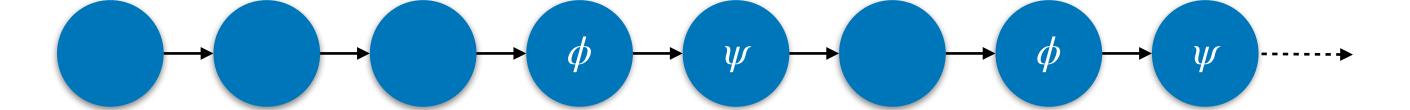
always ( $\phi$  implies always  $\psi$ )



always ( $\phi$  implies eventually  $\psi$ )

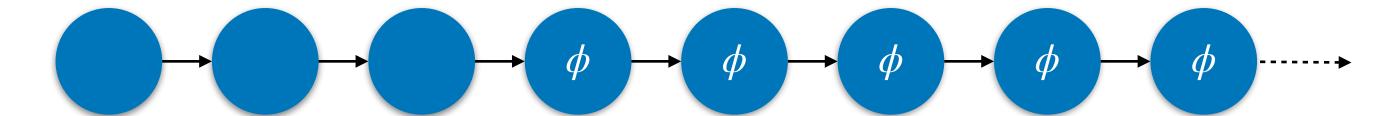


always ( $\phi$  implies after  $\psi$ )

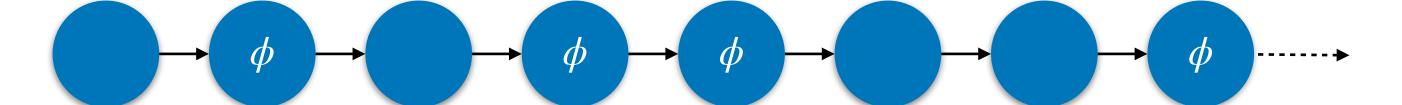


# Mixing operators

eventually (always  $\phi$ )



always (eventually  $\phi$ )



# Past temporal operators

```
historically \phi \phi was always true

once \phi \phi was once true

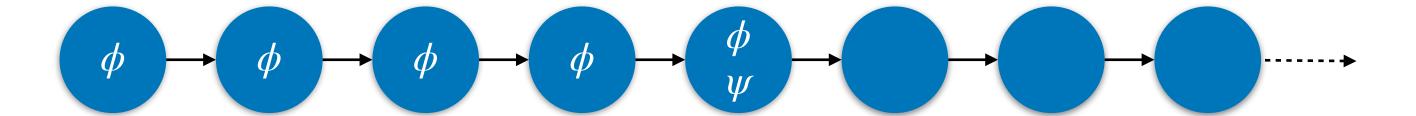
before \phi \phi was true in previous state

\psi since \phi \phi was once true and \psi was true since then

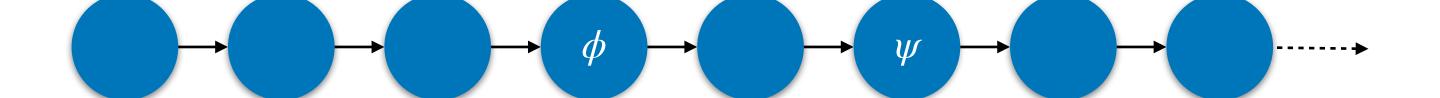
\phi triggered \psi \psi was always true back to the point where \phi was true
```

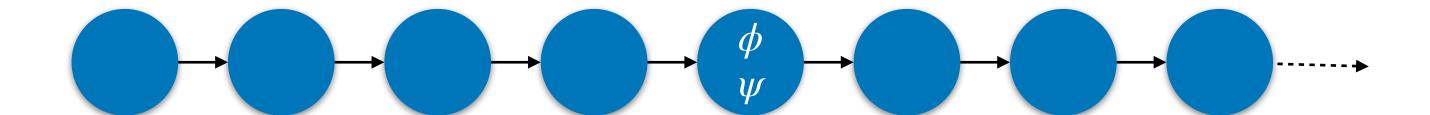
## Past operators

always ( $\psi$  implies historically  $\phi$ )

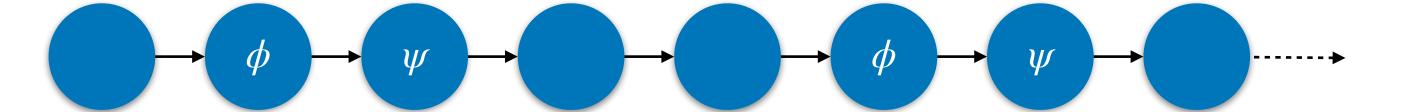


always ( $\psi$  implies once  $\phi$ )



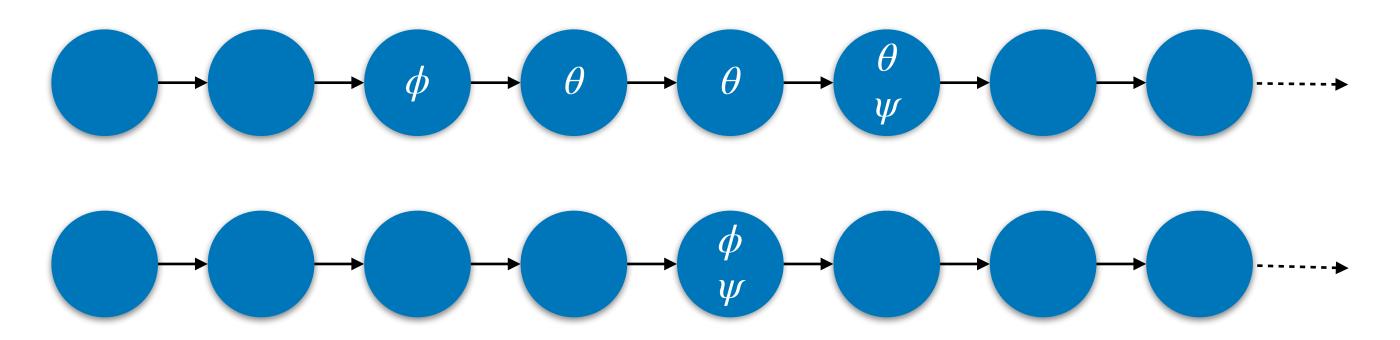


always ( $\psi$  implies before  $\phi$ )

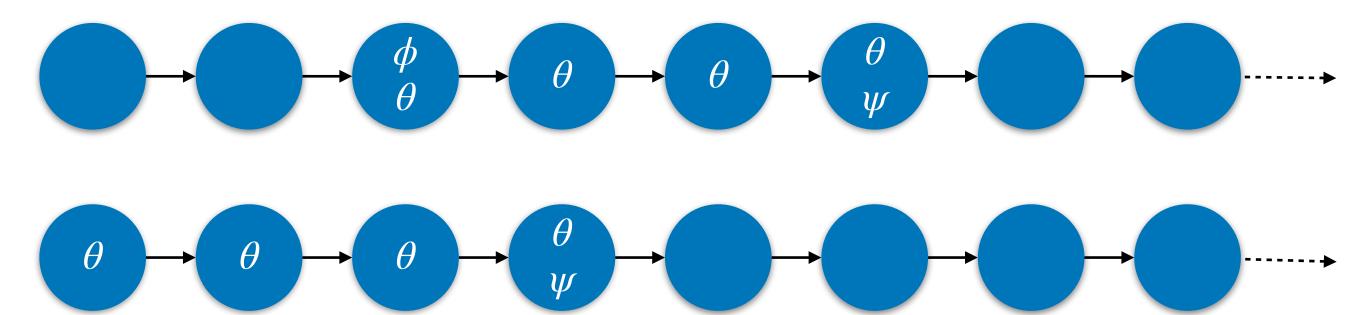


## Past operators

always ( $\psi$  implies  $\theta$  since  $\phi$ )



always ( $\psi$  implies  $\phi$  triggered  $\theta$ )



# Safety properties

- Safety properties prevent some undesired behaviors from happening
  - Easier to model check, since it suffices to search for a finite sequence of steps that leads to a bad state
  - It is irrelevant what happens afterwards, and any continuation leads to a counter-example
  - The archetypal safety property is an *invariant* specified as **always**  $\phi$

## Liveness properties

- Liveness properties force some desired behaviors to happen
  - Harder to model check, since it is necessary to search for a complete infinite trace where the desired behavior never happened
  - Harder to specify, since they require fairness assumptions that prevent the system from stuttering forever
  - The archetypal liveness property is eventually  $\phi$

# Some operational principles

```
check invariant {
   // No item can simultaneously be accessible and trashed
   always no Accessible & Trashed
check restore after delete {
   // A restore is only possible after a delete
   all x : Item | always (restore[x] implies once delete[x])
check accessible after delete {
   // A deleted item only becomes accessible again after being restored or created
   all x : Item | always {
      delete[x] implies after {
          (restore[x] or create[x]) releases x not in Accessible
```

# The key operational principles

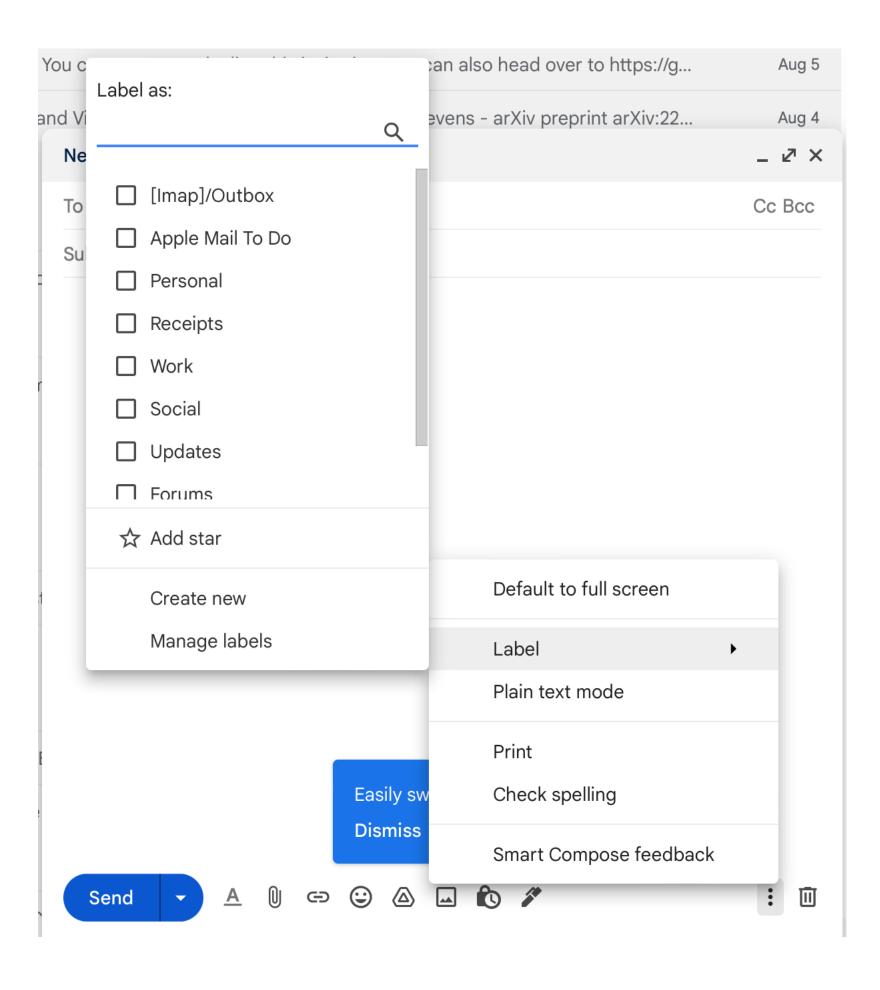
```
pred can restore [x : Item] { x in Trashed }
check delete_restore {
    // After delete(x), can restore(x) and then x in accessible
    all x : Item | always {
       delete[x] implies after can_restore[x]
        (delete[x]; restore[x]) implies x in Accessible''
} for 4 Item, 20 steps
pred can_empty { some Trashed }
check delete_empty {
    // After delete(x), can empty() and then x not in accessible or trashed
    all x : Item | always {
       delete[x] implies after can empty
       delete[x] and after empty implies x not in (Trashed+Accessible)''
} for 4 Item, 20 steps
```

### Verification

```
8 commands were executed. The results are:
    #1: Instance found. Scenario1 is consistent, as expected.
    #2: No instance found. Scenario2 may be inconsistent, as expected.
    #3: Instance found. Scenario3 is consistent, as expected.
    #4: No counterexample found. invariant may be valid.
    #5: No counterexample found. restore_after_delete may be valid.
    #6: No counterexample found. accessible_after_delete may be valid.
    #7: No counterexample found. delete_restore may be valid.
    #8: No counterexample found. delete_empty may be valid.
```

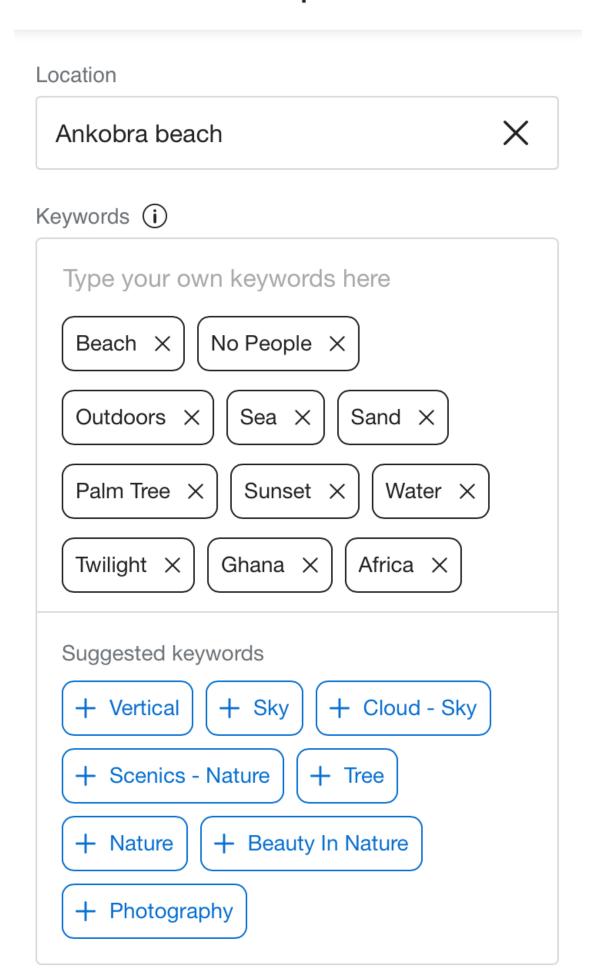


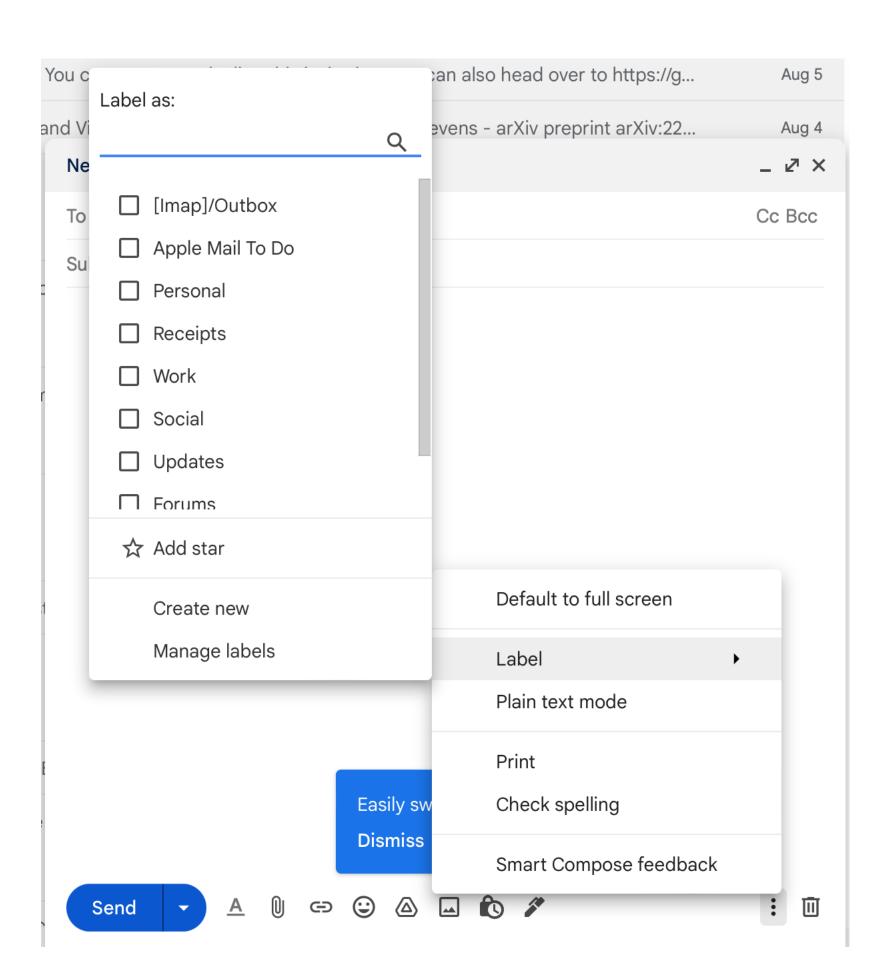
# Another concept



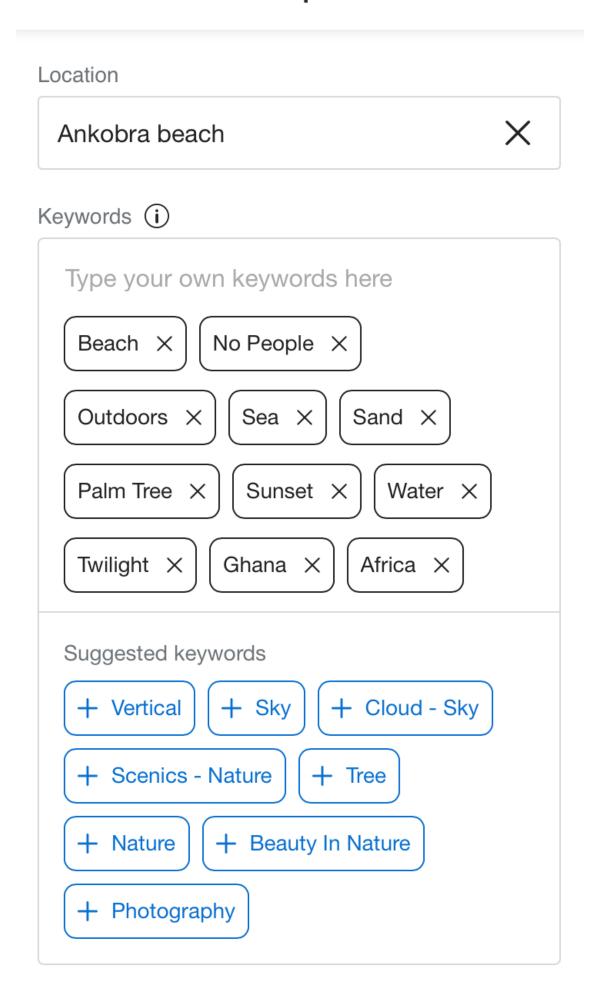
#### You c an also head over to https://g... Aug 5 Label as: evens - arXiv preprint arXiv:22... and Vi Aug 4 Ne \_ 2 X ☐ [Imap]/Outbox Cc Bcc ☐ Apple Mail To Do Personal ☐ Receipts ☐ Work Social Updates ☐ Forums ☆ Add star Default to full screen Create new Manage labels Label Plain text mode Print Check spelling Easily sv **Dismiss** Smart Compose feedback Send - A () C () A () /

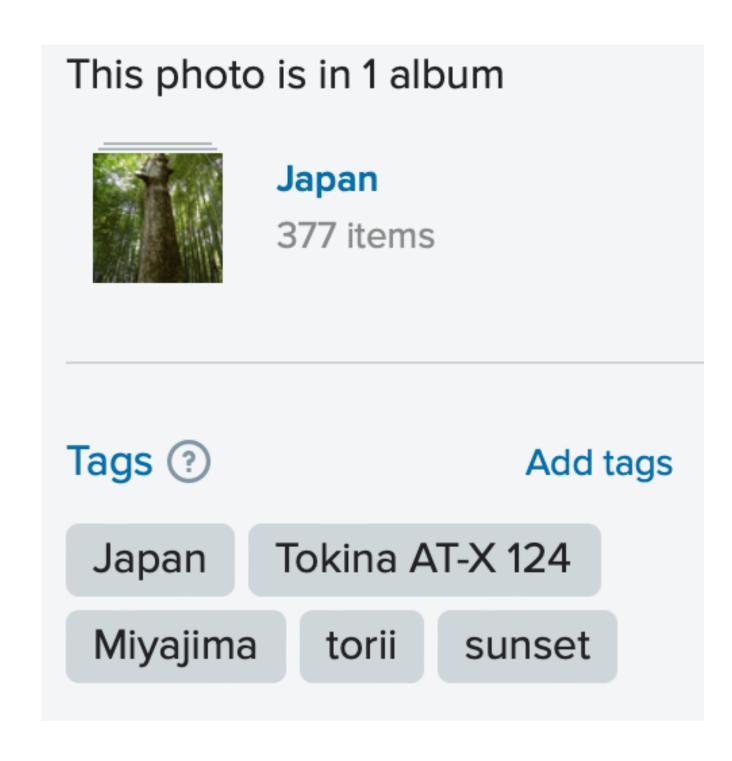
#### **Edit 1 photo**





#### **Edit 1 photo**





# Label modeling a la Jackson

```
concept label [Item]
purpose
  organize items into overlapping categories
state
  labels : Item -> set Label
actions
  affix (i : Item, l : Label)
    when 1 not in the labels of i
    add 1 to the labels of i
  detach (i : Item, l : Label)
    when l in the labels of i
    remove 1 from the labels of 1
  clear (i : Item)
    when i has some labels
    remove all labels of i
operational principle
  after affix(i,1), while no detach(i,1) and no clear(i), i is in the labels of 1
```

## The label in Alloy

```
sig Item {
 var labels : set Label
sig Label {}
fact Behavior {
 no labels
  always {
    (some i : Item, l : Label | affix[i,l] or detach[i,l])
    or
    (some i : Item | clear[i])
    or
    stutter
```

# Affix label with point-wise effect

```
pred affix [i : Item, l : Label] {
    // guard
    l not in i.labels
    // effect
    i.labels' = i.labels + l
    // frame condition
    all j : Item - i | j.labels' = j.labels
}
```

## Affix label with point-free effect

```
pred affix [i : Item, l : Label] {
    // guard
    l not in i.labels
    // effect
    labels' = labels + i->l
}
```

### Detach label

```
pred detach [i : Item, l : Label] {
    // guard
    l in i.labels
    // effect
    labels' = labels - i->l
}
```

### Clear item

```
pred clear [i : Item] {
    // guard
    some i.labels
    // effect
    labels' = labels - i->Label
}
```

### Label scenarios

```
run Scenario1 {
  some i : Item, disj l,m : Label {
    affix[i,l]; affix[i,m]; clear[i]
} expect 1
run Scenario2 {
  some i : Item, l : Label {
    affix[i,l]; affix[i,l]
} expect 0
```

# Label operational principle

```
check affix_find {
    // after affix(i,l), while no detach(i,l) and no clear(i), i is in the labels of l
    all i : Item, l : Label | always {
        affix[i,l] implies after ((detach[i,l] or clear[i]) releases l in i.labels)
    }
}
```

# App design

# Modularizing concepts

- To enable reuse and instantiation each concept should be in a parametrized module
- The module can still be used on its own, as Alloy implicitly declares parameter signatures
- Since a parameter signature cannot be extended with new fields, some tricks might be necessary to declare them

### Trash

```
module Trash [Item]

sig Item {}
var sig Accessible in Item {}
var sig Trashed in Item {}
...
```

```
module Label [Item]
sig Item {
 var labels : set Label
sig Aux in Item {
  var labels : set Label
fact { Aux = Item }
sig Label {}
```

• • •

# Specifying apps

- Import the required concepts, instantiating parameter signatures as needed
- Compose the concepts
  - Enforce interleaving, by requiring at most one concept not to stutter
  - Synchronize actions as needed
- Validate, validate, validate
- Check some expected properties

# A filesystem app

- Composed of trash and label
- Many options to explore
  - When to allow affixing labels?
  - When to delete labels?
  - Whether to use special labels?

#### Free composition

```
open Trash[File] as trash
open Label[File] as label
sig File {}
fact Interleave {
  always {
    trash/stutter or
    label/stutter
run Example {}
```

- Allow labelling only when accessible
- Clear labels when file is deleted

```
fact Synchronization {
    // allow affixing only if file is accessible
    all f : File, l : Label | always (affix[f,l] implies f in Accessible)

    // clear all labels after file is deleted
    all f : File | always (delete[f] and some f.labels implies after clear[f])
}
```

```
run Scenario1 {
  some f : File, l : Label {
    create[f]; affix[f,l]; delete[f]
} expect 1
run Scenario2 {
  some f : File, l : Label {
    create[f]; delete[f]; affix[f,l]
} expect 0
```



- Allow labelling when accessible or trashed
- Clear labels when trash is emptied

```
fact Synchronization {
  // allow labelling when accessible or trashed
  all f : File, l : Label | always (affix[f,l] implies f in Accessible+Trashed)
  // clear labels when trash is emptied
  always {
    empty implies after {
     (some f : File-Accessible | clear[f]) until no (File-Accessible).labels
```

```
run Scenario1 {
  some f : File, l : Label {
    create[f]; affix[f,l]; delete[f]
} expect 1
run Scenario2 {
  some f : File, l : Label {
    create[f]; delete[f]; affix[f,l]
expect 1
```

```
run Scenario3 {
   some f : File, l : Label {
       create[f]; delete[f]; empty; affix[f,l]
} expect 0
run Scenario4 {
   some disj f1,f2 : File, l : Label {
       create[f1]; create[f2]; delete[f1]; affix[f2,1]; delete[f2]; affix[f1,1]; empty
} expect 1
run Scenario5 {
   some disj f1,f2 : File, l : Label {
       create[f1]; delete[f1]; affix[f1,1]; empty; create[f2]
} expect 0
```



- Allow labelling when accessible or trashed
- Clear labels when trash is emptied
- Affix special label Trashed when file is deleted
- Detach special label Trashed when file is restored

```
one sig Dirty extends Label {}
fact Synchronization {
  // allow labelling when accessible or trashed
  all f : File, l : Label | always (affix[f,l] implies f in Accessible+Trashed)
  // clear labels when trash is emptied
  always {
    empty implies after ((some f : File-Accessible | clear[f]) until no (File-Accessible).labels)
  // affix label Trashed after delete
  all f : File | always (delete[f] and Dirty not in f.labels implies after affix[f,Dirty])
  // detach label Trashed after restore
  all f : File | always (restore[f] and Dirty in f.labels implies after detach[f,Dirty])
```



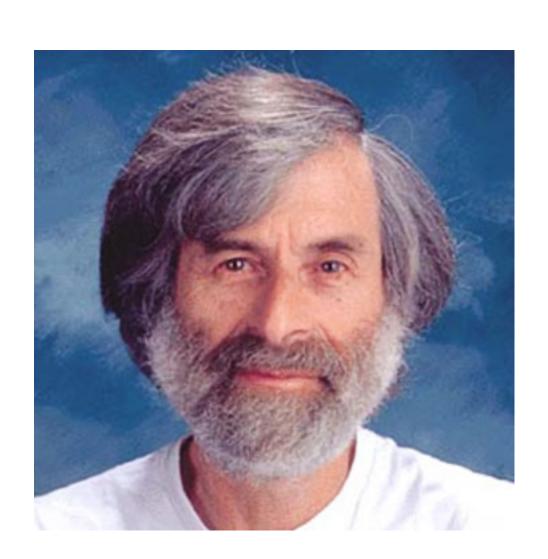
## Epilogue

# "Software is built on abstractions. Pick the right ones, and programming will flow naturally from design [...] Pick the wrong ones, and programming will be a series of nasty surprises"



-Daniel Jackson

"A specification is an abstraction. [...] But I don't know how to teach you about abstraction. A good engineer knows how to abstract the essence of a system and suppress the unimportant details when specifying and designing it. The art of abstraction is learned only through experience."



-Leslie Lamport

"There are two ways of constructing a software design: One way is to make it so simple that there are obviously no deficiencies, and the other way is to make it so complicated that there are no obvious deficiencies.

The first method is far more difficult."



-Tony Hoare

Epigram 31
"Simplicity does not precede complexity, but follows it."



-Alan Perlis

#### always eventually some Alloy